



the framework of:  
**Probabilistic Functional Modes**

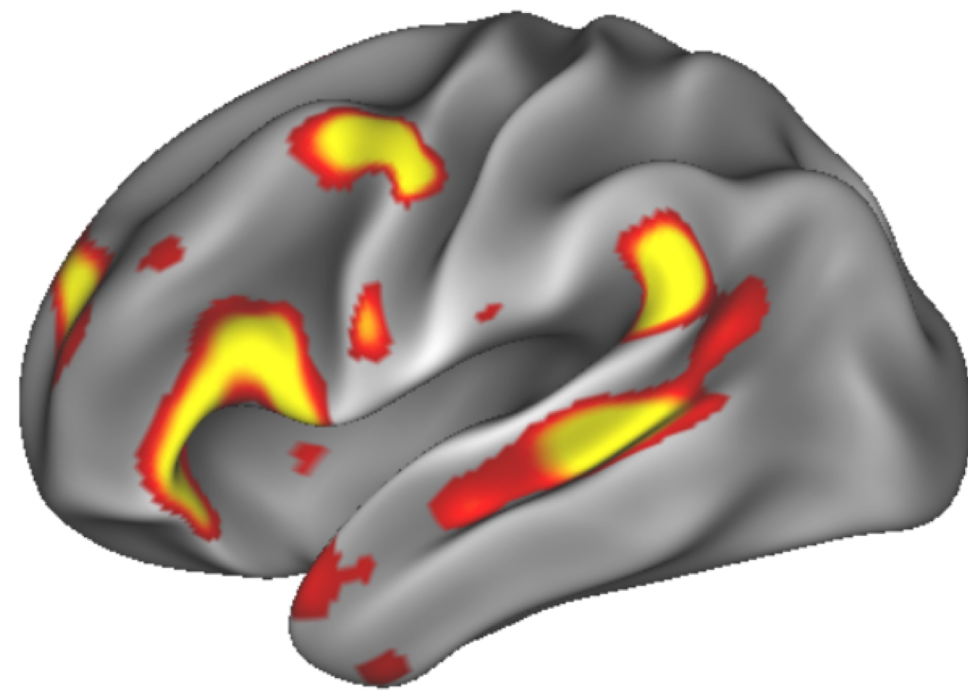
*part 1*



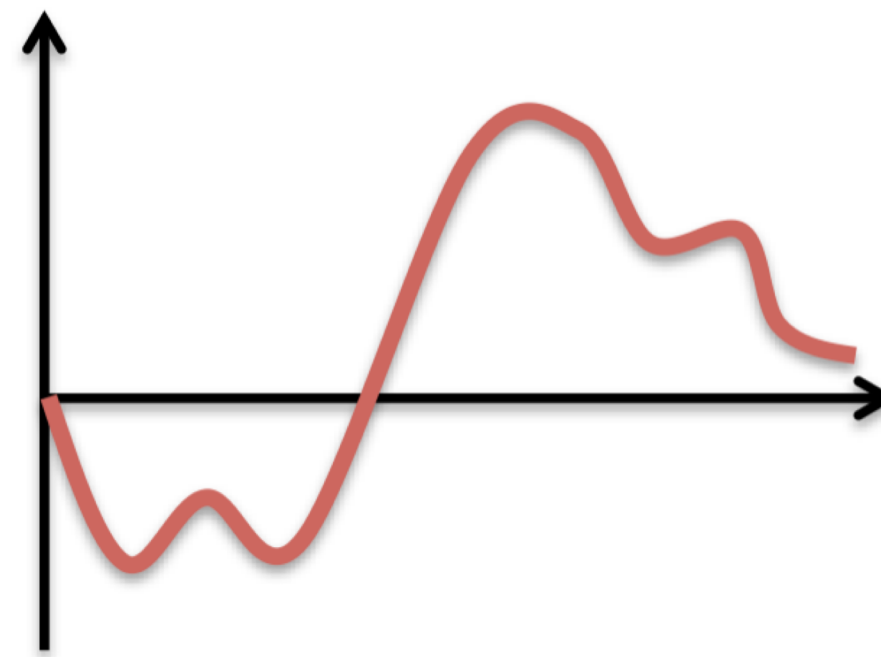
- Description of PFM framework and its key features.
- PFM Network Matrices, comparison to ICA, and interpretability of functional connectivity.
- PFMs for big data and prediction of individualistic traits.



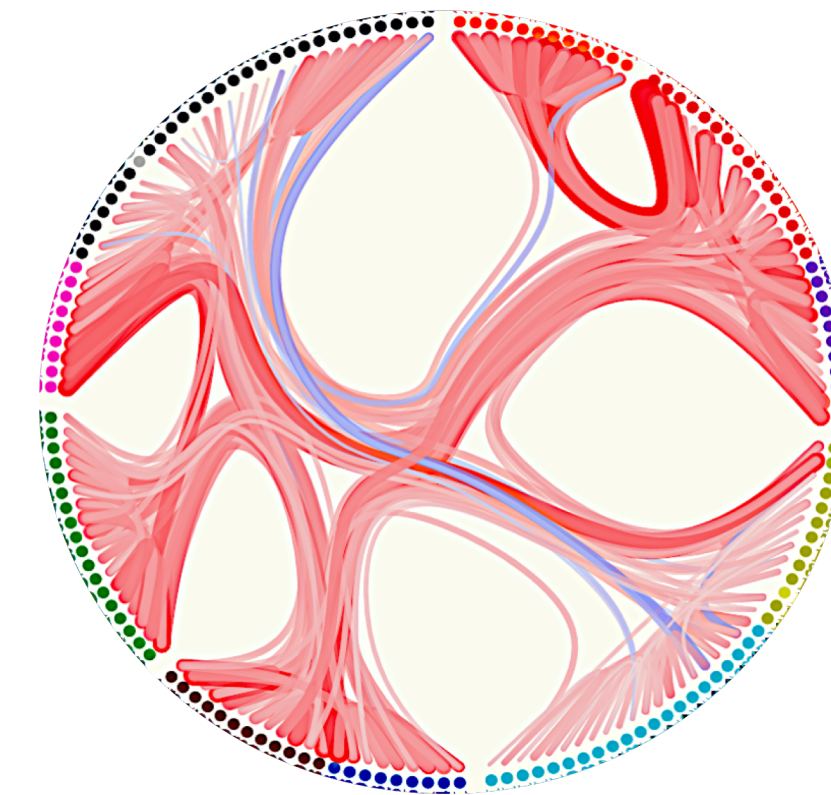
Spatial Configuration  
(Topography)



Time Courses



Temporal Correlation  
(Functional Connectivity)

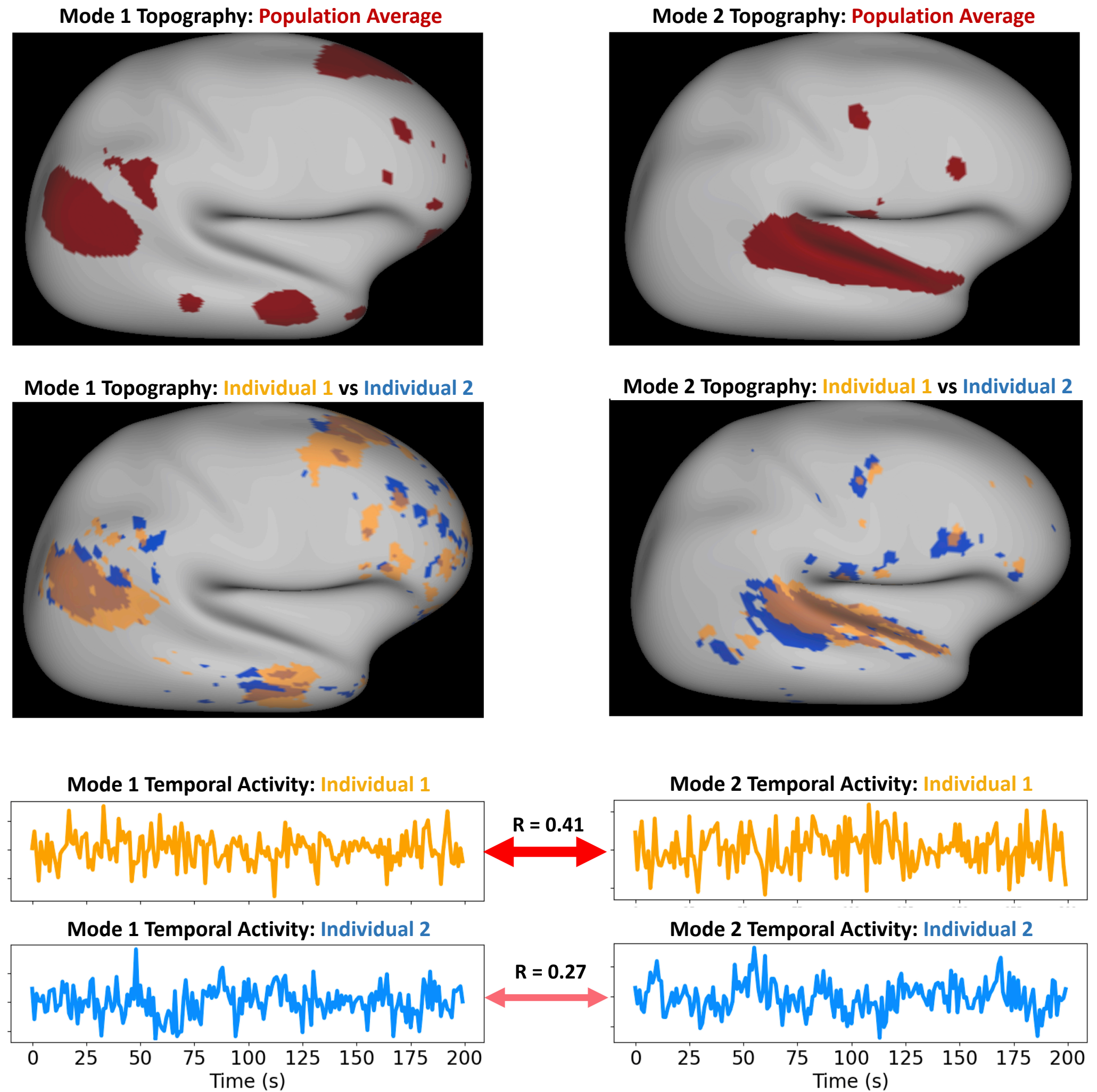


- Functional mode -> a set of brain regions that share a common time course.
- Can be estimated from resting-state data (i.e., resting-state networks or RSNs) or task data.

# Functional modes vary across individuals



- Inter-subject variability of **networks topographies** and **functional connectivity** is meaningfully predictive of personalised traits and pathology, like a diagnostic assay for the brain.

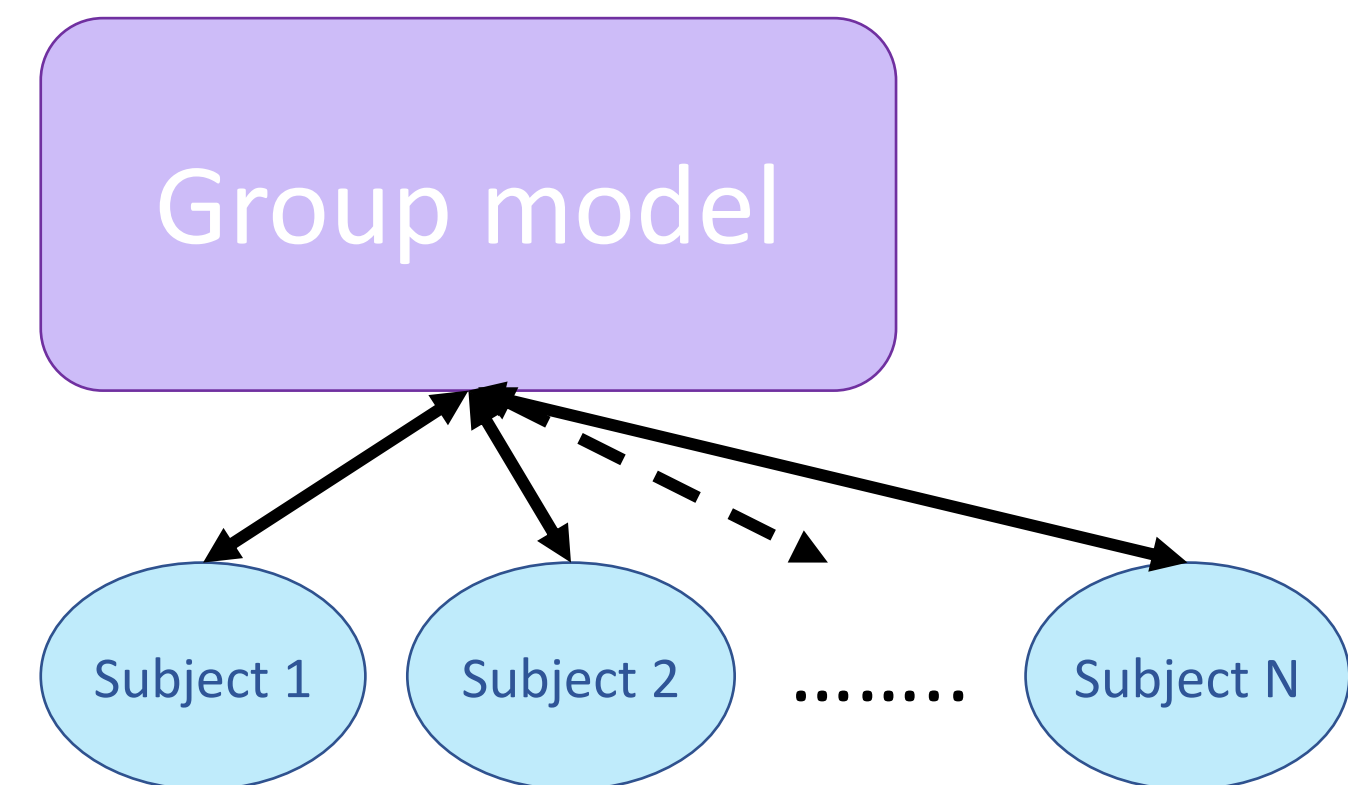
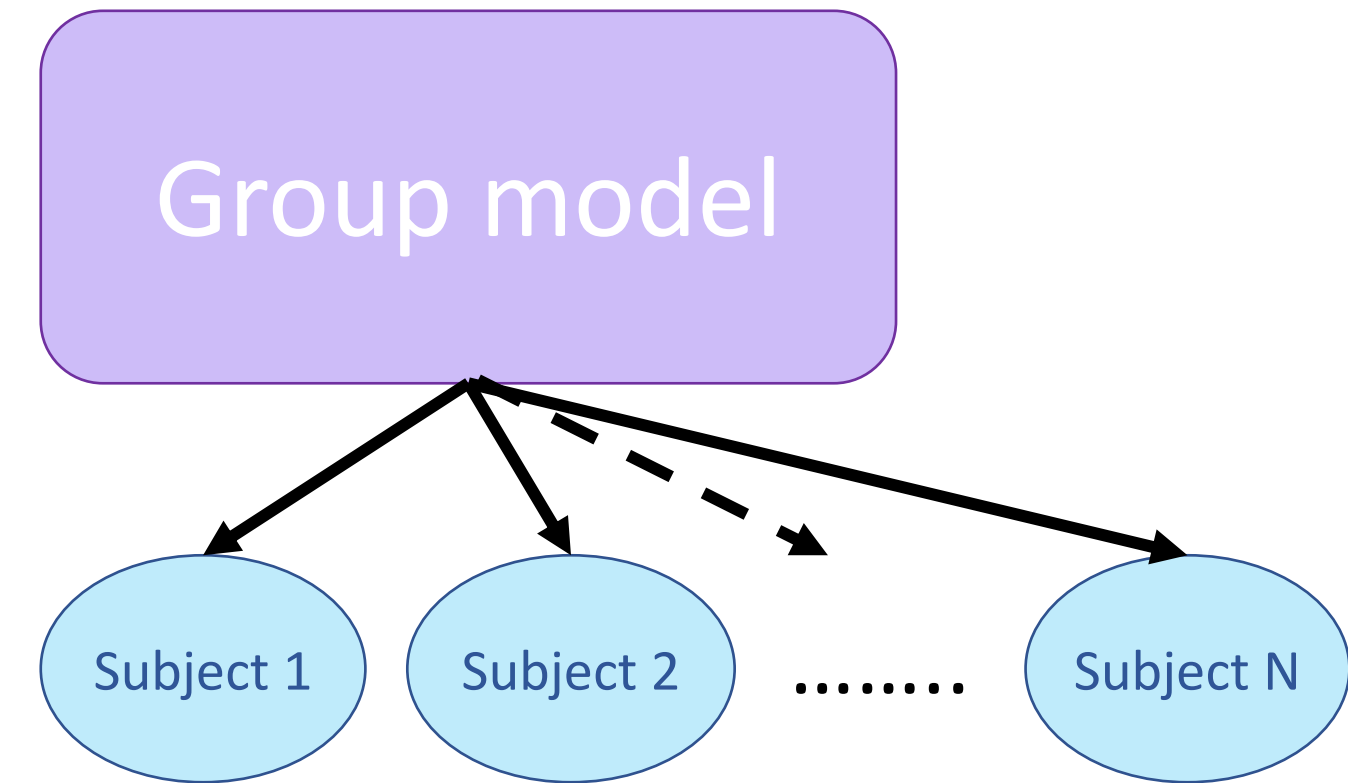


# Current standard technique: Group ICA + Dual Regression



- Subject-specific mode estimation typically follows two separate steps:
  1. Group-level ICA
  2. Group-ICA mapped onto subject fMRI timeseries via multiple regressions
- Explicit subject modelling: No
- Directionality: Unidirectional
- Limited ability for capturing cross-individual variability

➤ Recent advances include estimating modes simultaneously and hierarchically for the population and individuals

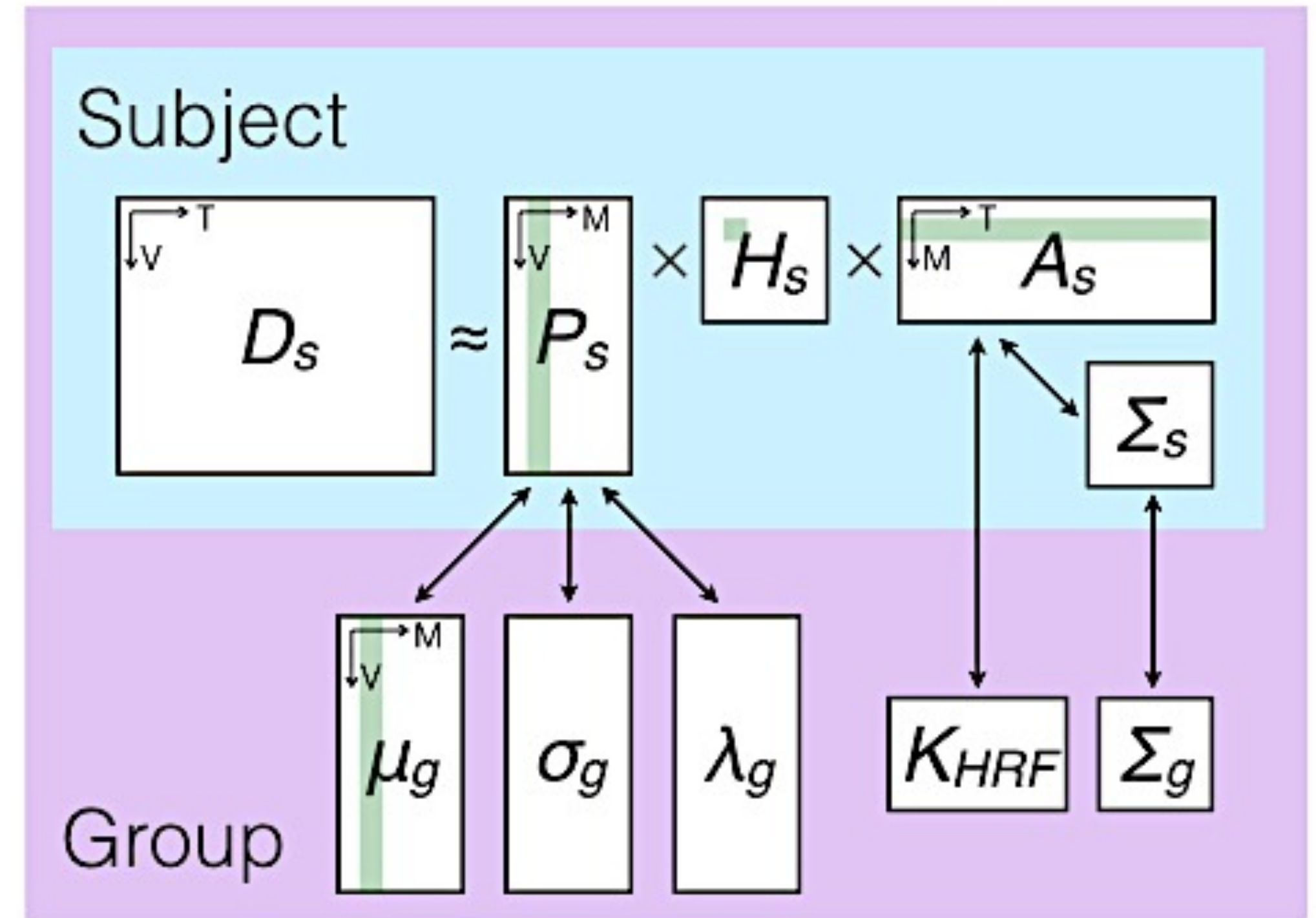




# Probabilistic Functional Modes (PFMs)



- Simultaneous modelling of population and individuals
  1. Group-level modes used for top-down regularisation of individuals
  2. Individual-specific modes used for bottom-up regularisation of the group
- Explicit subject modelling: Yes
- Directionality: Bidirectional
- Aim is to improve cross-individual variability modelling



Based on Harrison et al., 2015

How does the model work?

# Reconstructing functional modes using Matrix Factorisation



- FMRI data ( $N_{\text{Voxel}} \times N_{\text{Time}}$ ) is factorised into a set of functional modes. Modes are characterised by:

## 1. Spatial Maps ( $N_{\text{Voxel}} \times N_{\text{Mode}}$ )

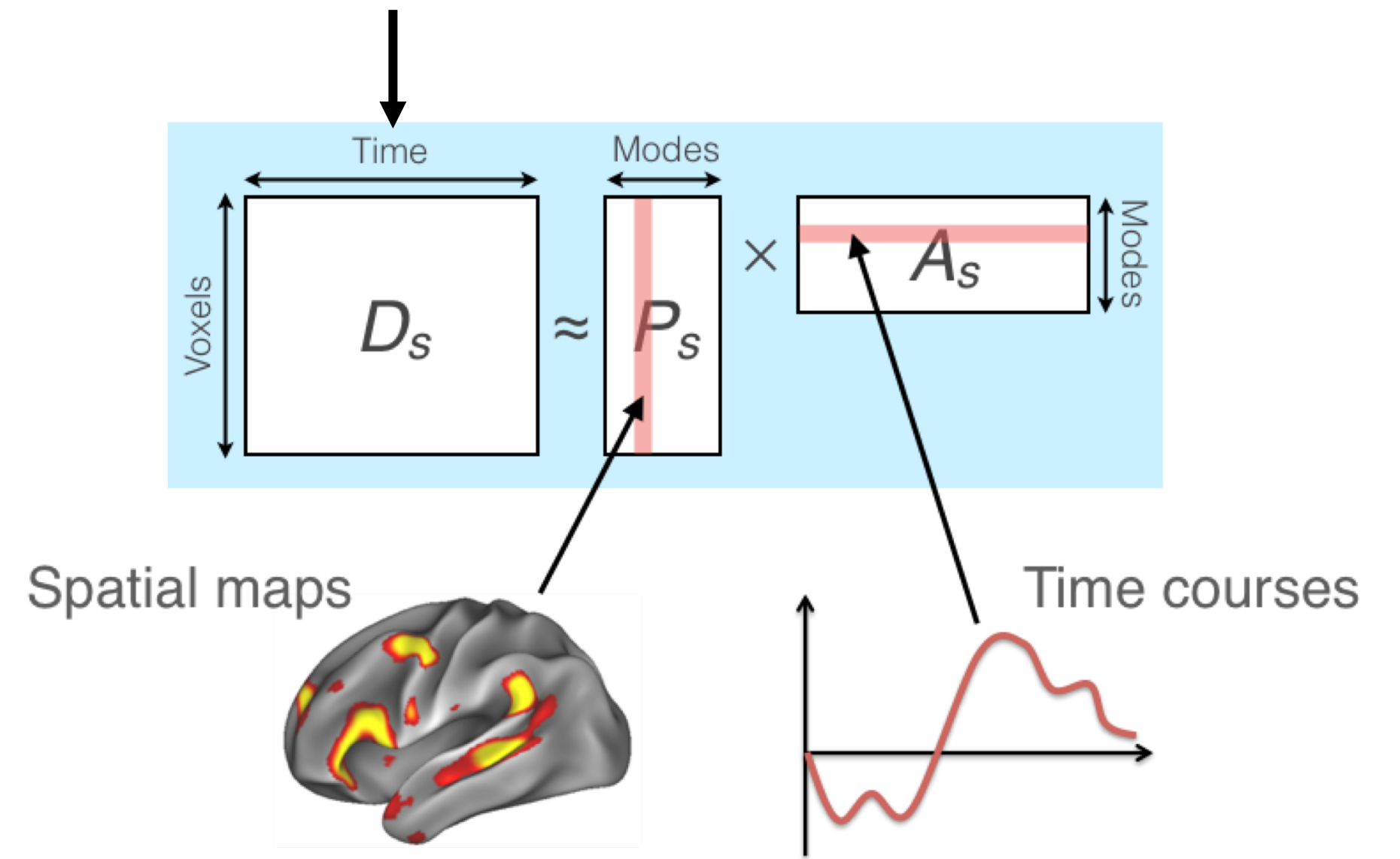
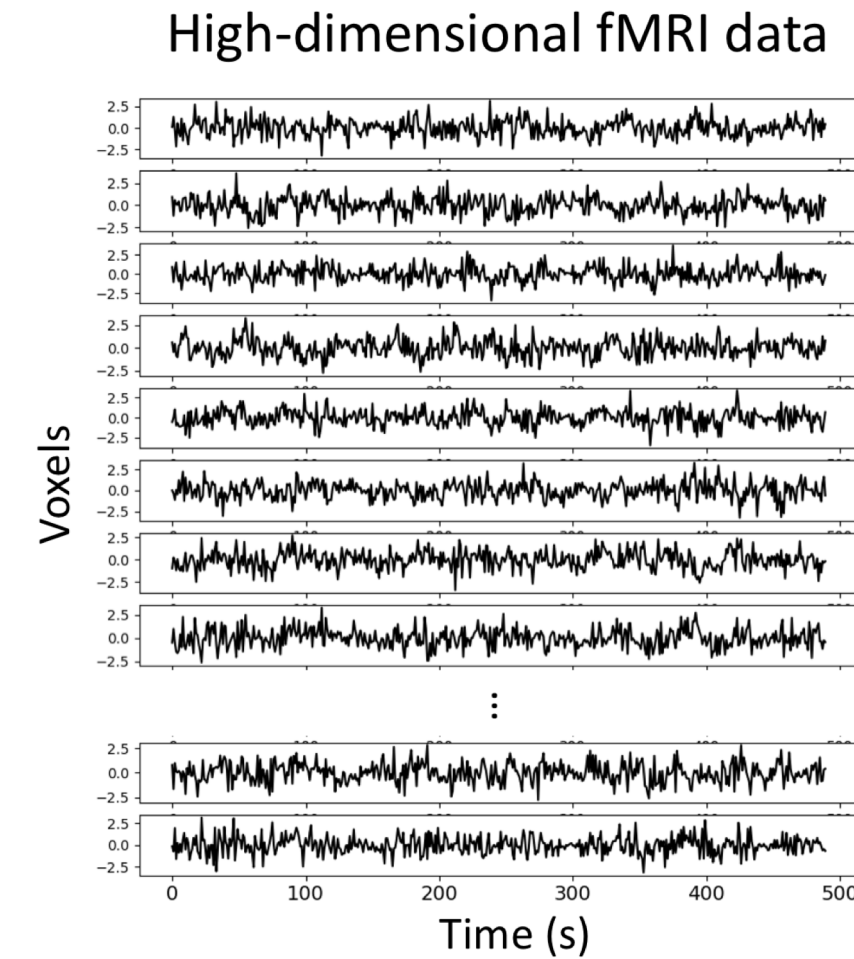
- Spatial configuration or Topography

## 2. Time course ( $N_{\text{Mode}} \times N_{\text{Time}}$ )

- Activity over time

## 3. Functional Connectivity ( $N_{\text{mode}} \times N_{\text{mode}}$ )

- Temporal correlation between modes (NetMat)



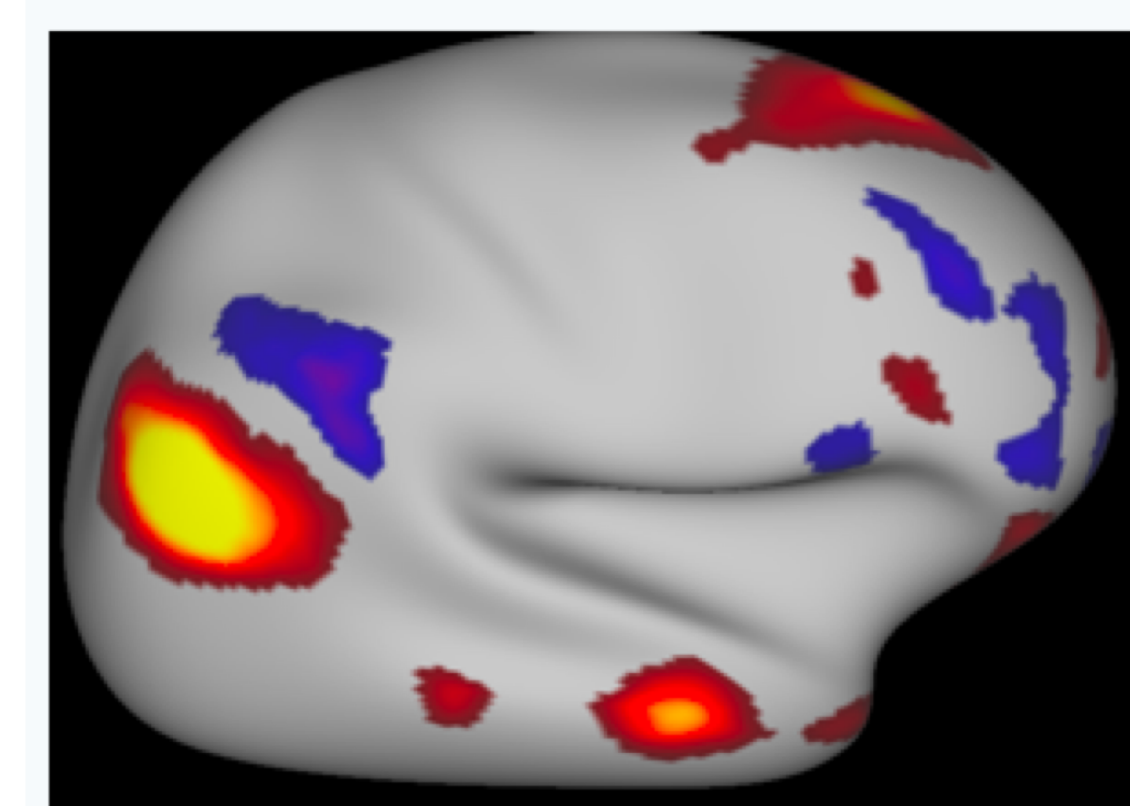
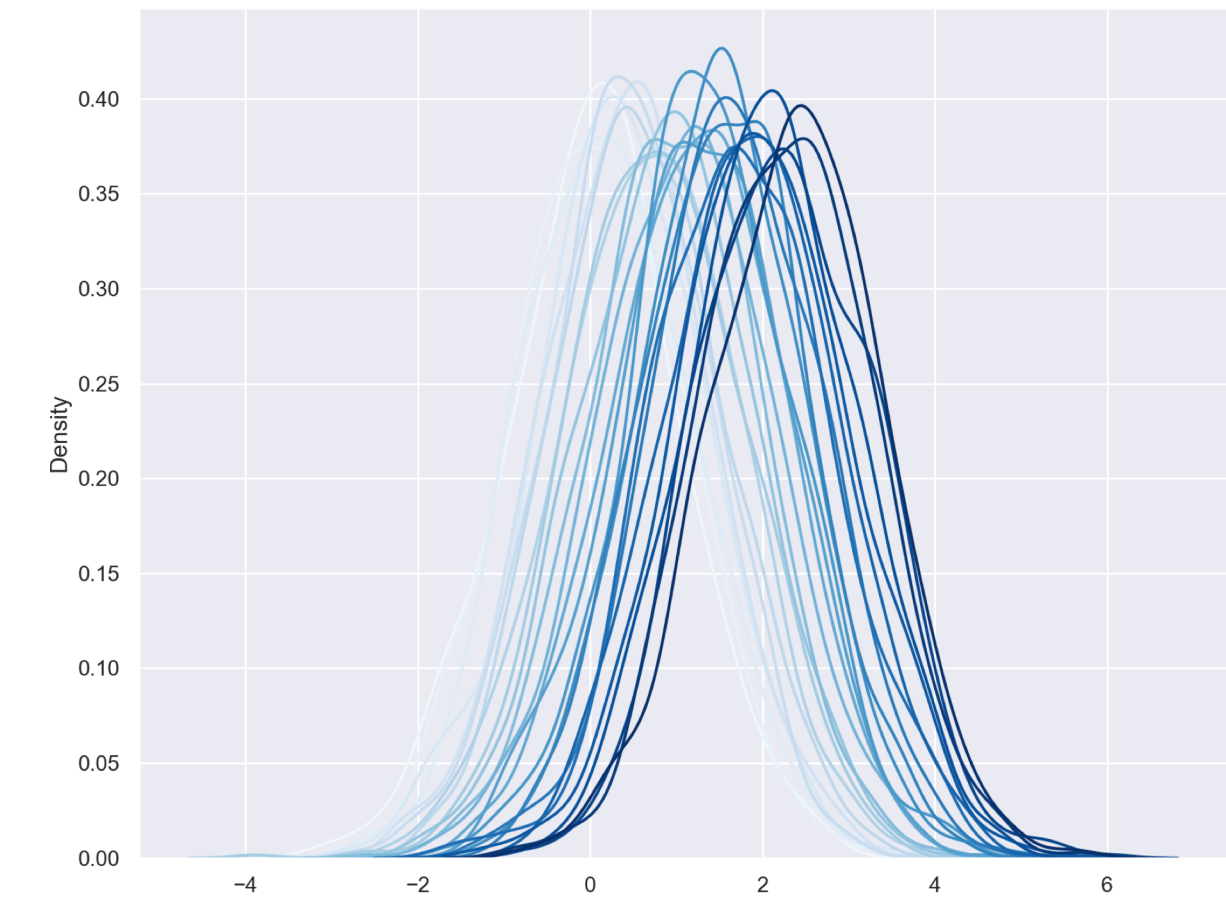


- Let us assume that we have fMRI data from a subject 's' and recording session 'r'.
- We do the following matrix factorisation for this subject:

$$\mathbf{D} = \mathbf{P} \mathbf{H} \mathbf{A} + \boldsymbol{\varepsilon} \quad (1)$$

- Where:  $\mathbf{D}$  -> preprocessed data;
- $\mathbf{P}$  -> spatial maps of modes;
- $\mathbf{A}$  -> time courses of modes;
- $\mathbf{H}$  -> amplitudes of mode activity over time;
- $\boldsymbol{\varepsilon}$  -> residuals;
- $\alpha$  -> partial temporal correlation (i.e., connectivity) between timeseries of  $\mathbf{A}$ .

- We use a data-driven probabilistic approach to approximate a solution to Equation 1.
- Our aim is to estimate a probability distribution for each of the model's spatial and temporal variables, for each subject and the group.
- For this purpose, we define what types of distributions we expect for each model element.
- For example, distributions for voxel-wise spatial maps are set to be Gaussian.
- Model should be able to estimate relevant parameters (e.g. mean and variance) to characterise these distributions to explain the observed data.

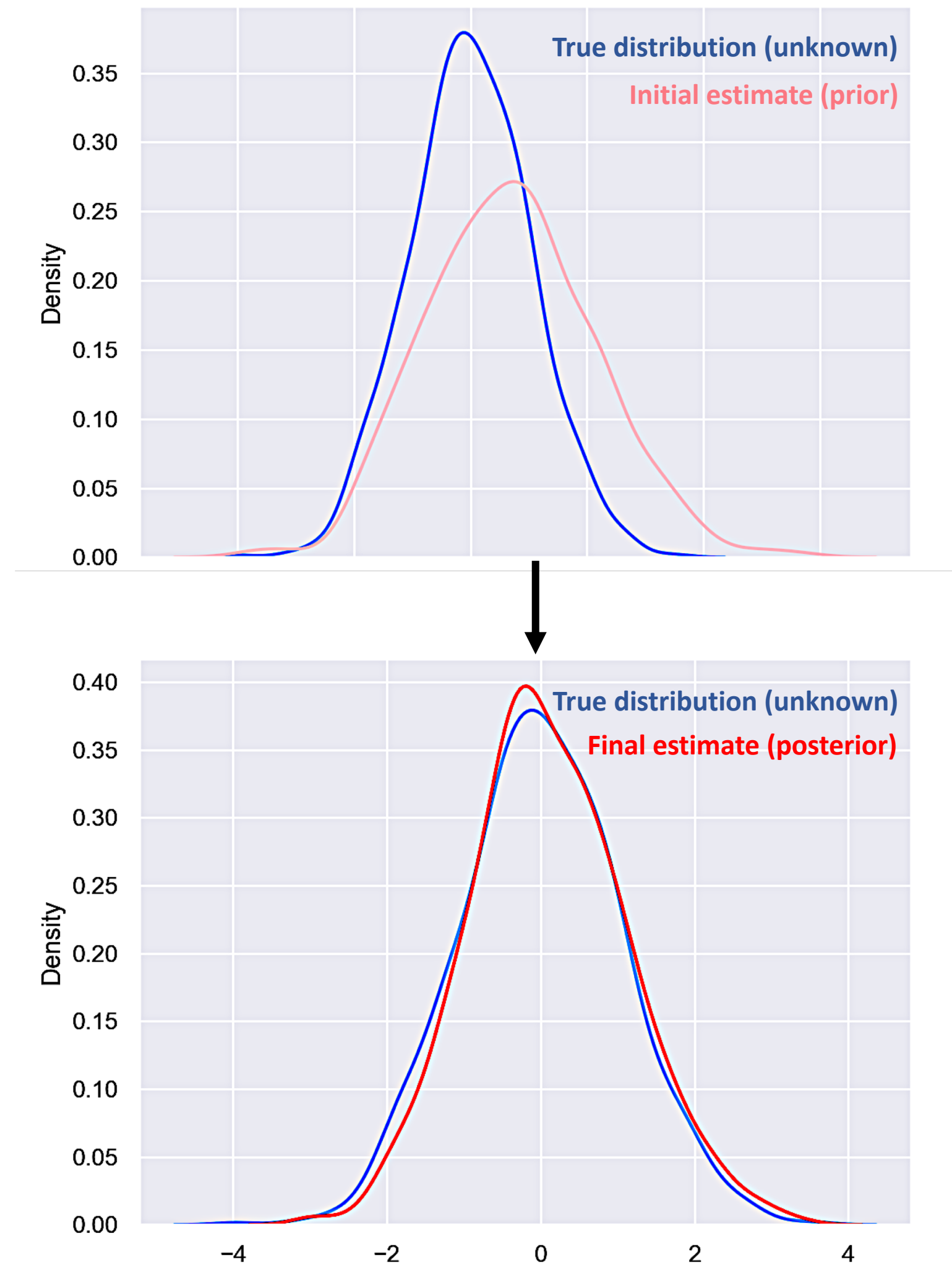




# Variational Bayesian solution to probabilistic framework



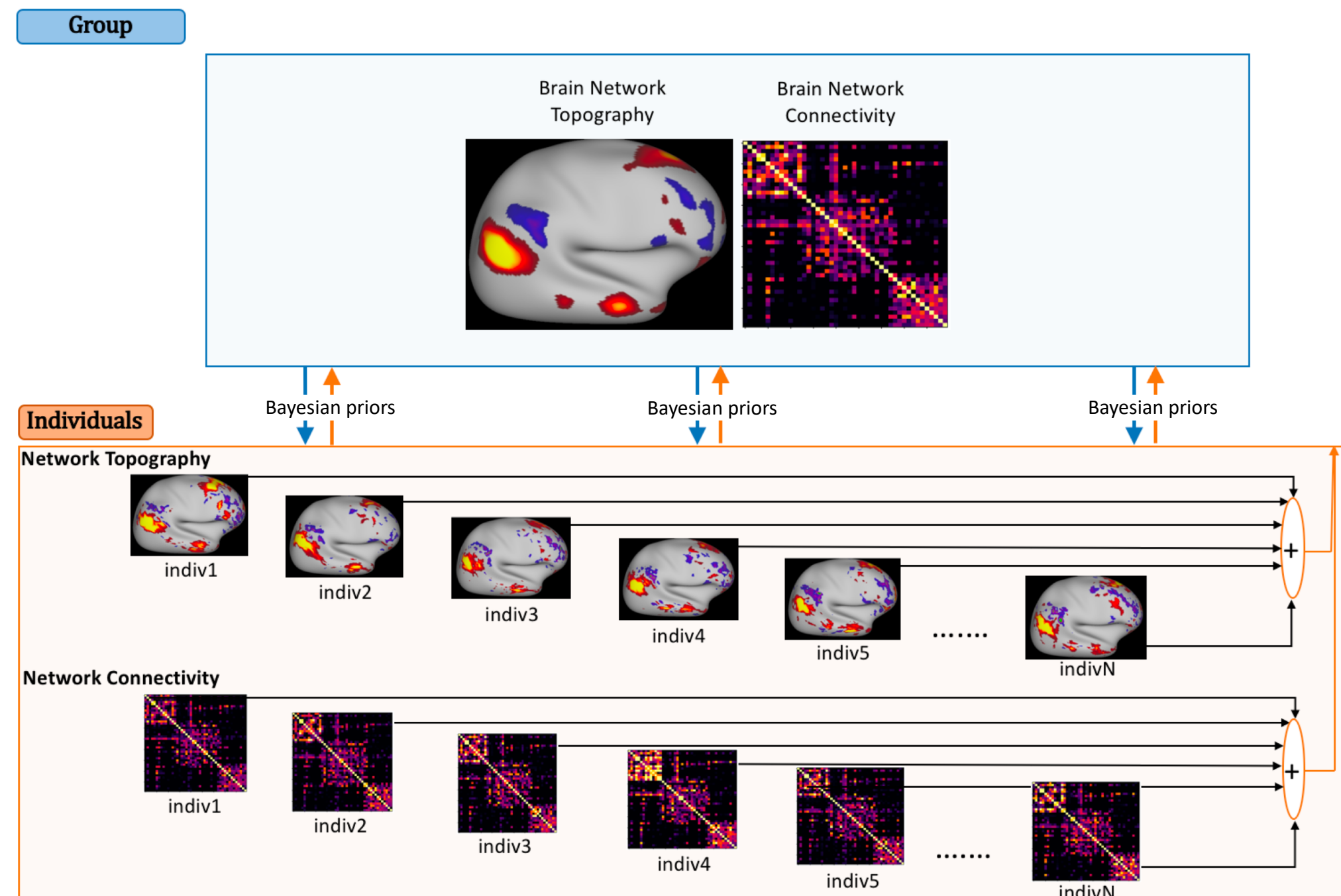
- To achieve this optimisation goal, we use Bayesian inference:
  1. Assume that there are "true" distributions in the data, which we do not know.
  2. We start with an initial estimate (prior).
  3. We optimise the distribution using a technique called variational Bayes (VB).
  4. Without knowing the true distribution, with VB inference we can derive and optimise a lower bound for the marginal likelihood of the data given the model (see Harrison et al., 2015 for technical details of inference).
- **Question: Where do we get the prior distributions from?**



# Hierarchical solution to the probabilistic Bayesian framework



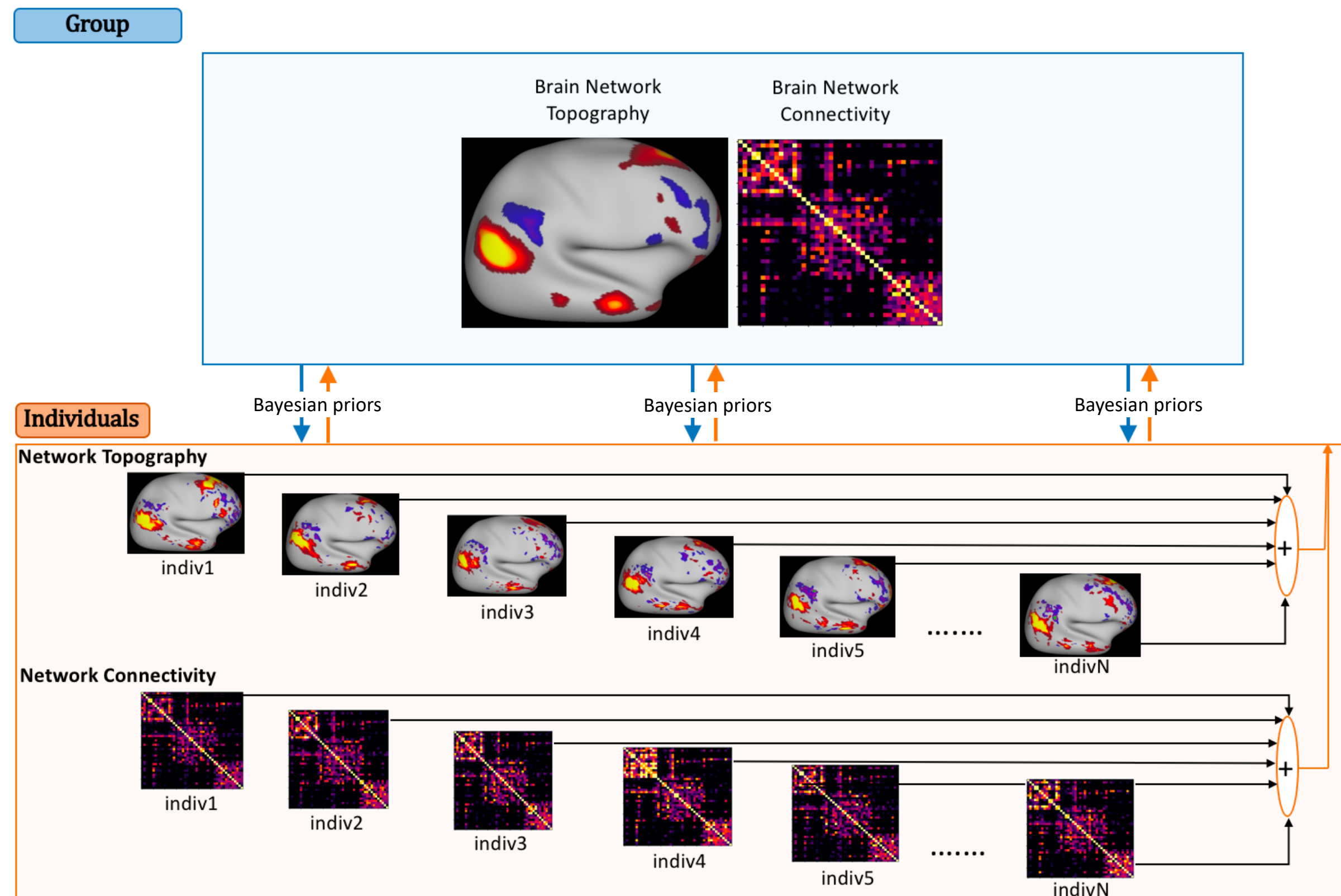
- Therefore, the model will:
  1. Compute an initial set of group-level modes
  2. Use priors from group-level modelling to regularise subject-specific estimations.
  3. Use accumulated posterior evidence across subject PFM's to update the group
  4. Iterate steps 2&3 until convergence



# Hierarchical solution to probabilistic framework



- To define the priors and optimise the subject-specific networks, the model works around these ideas:
  - The general spatial layout of the modes correspond across individuals, e.g. default mode network occupies roughly the same regions;
  - The general organisation of functional connectivity between the modes corresponds across individuals.
  - No group-level priors on time courses, but time course amplitudes are also defined hierarchically.



What are the key features of PFM?

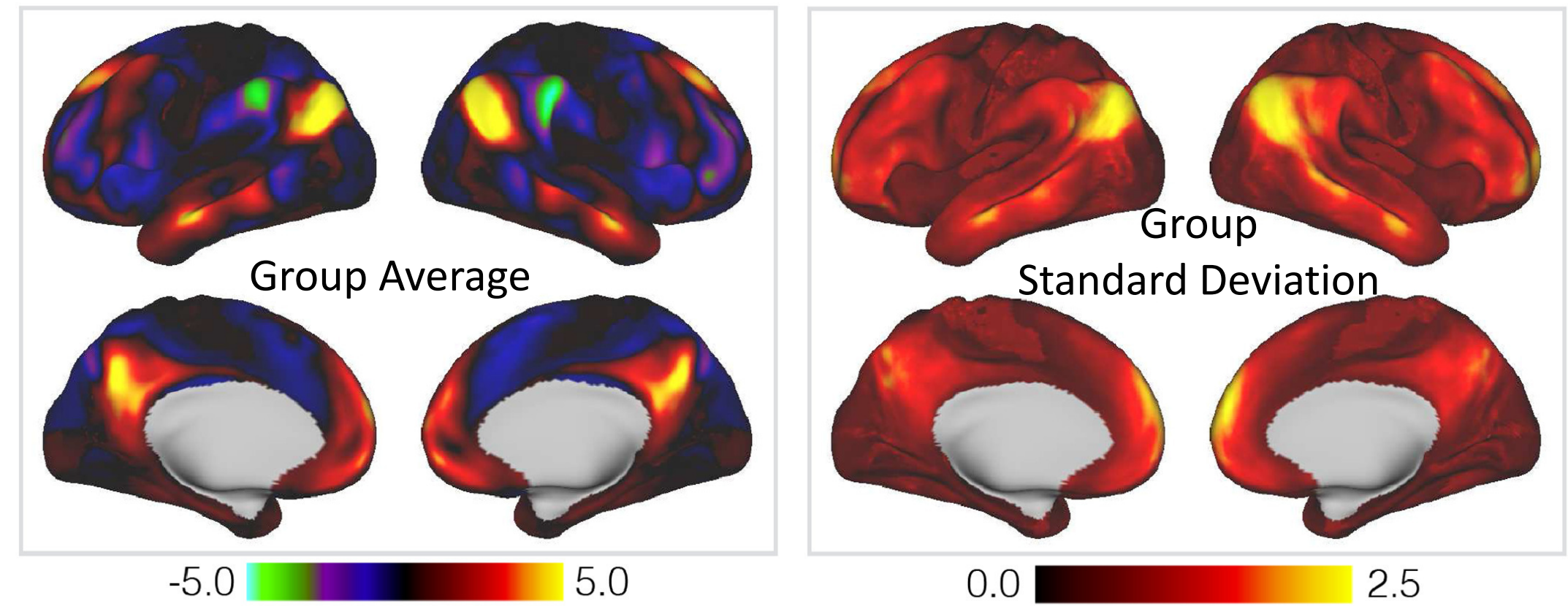


# 1) Simultaneous group and subject modelling

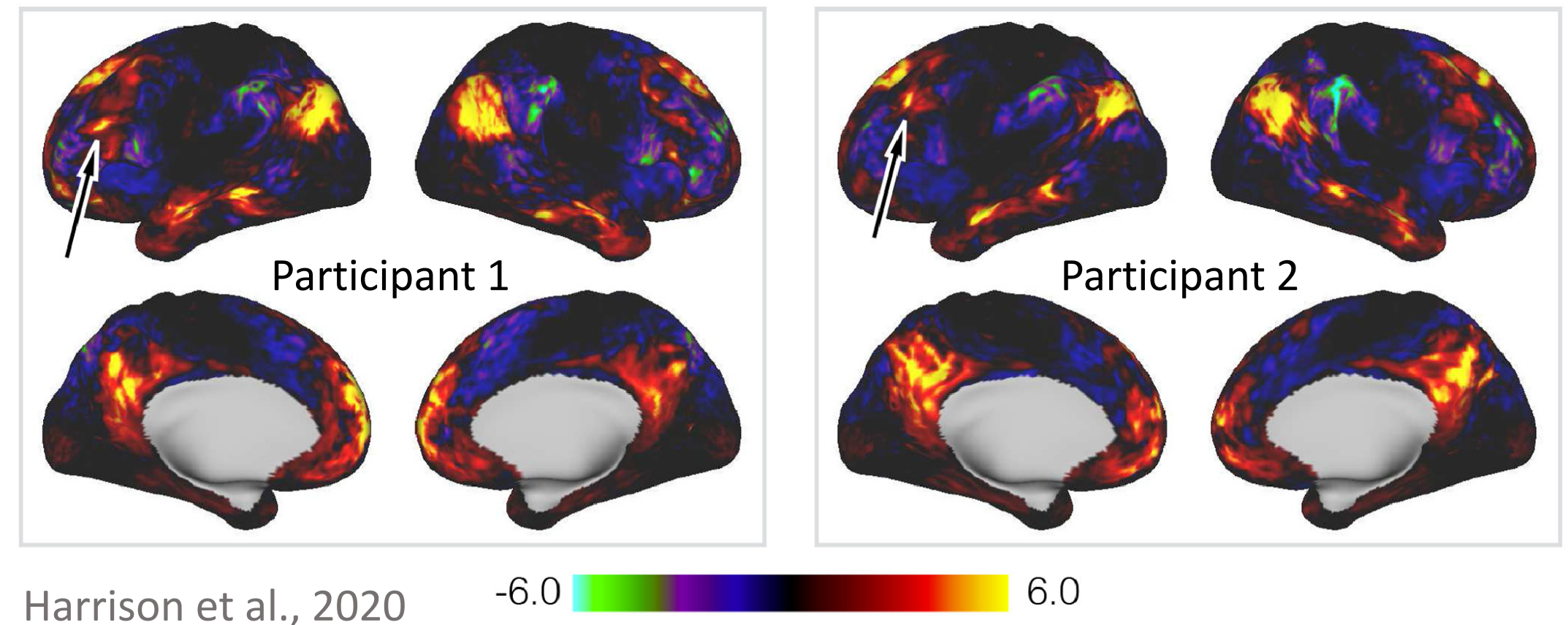


PfMs optimise group-level and subject-level mode estimations in a unified iterative process, which allows for bidirectional flow of information between population and individuals, leading to:

1. Group-model learning richer population variations



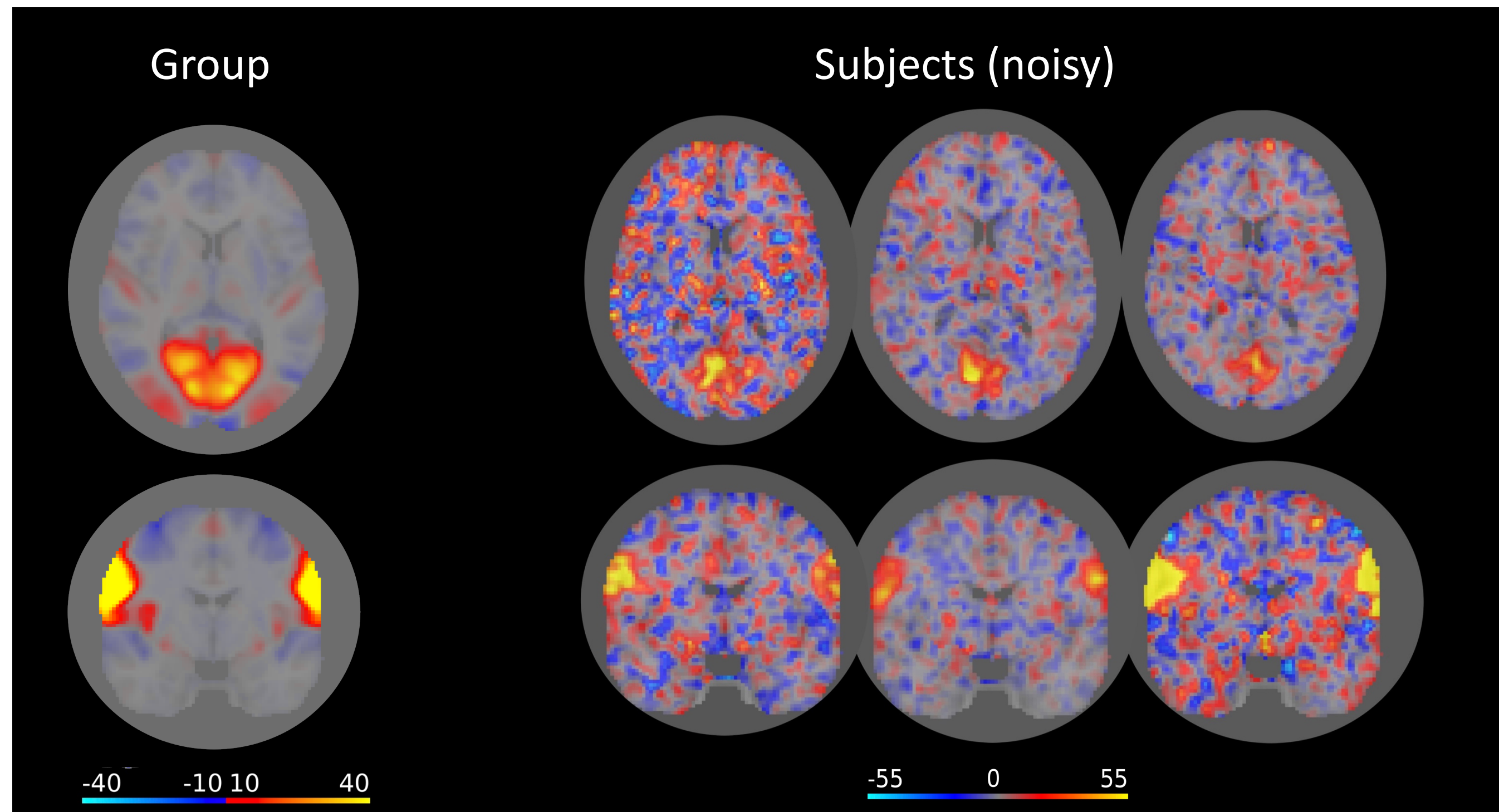
2. Accurate capturing of subject-specific deviations from the group







- Non-invasive recordings in fMRI means that data can be noisy
- In group-level estimations, noise can be cancelled by averaging across individuals
- Estimating clean modes for individual subjects can be very challenging



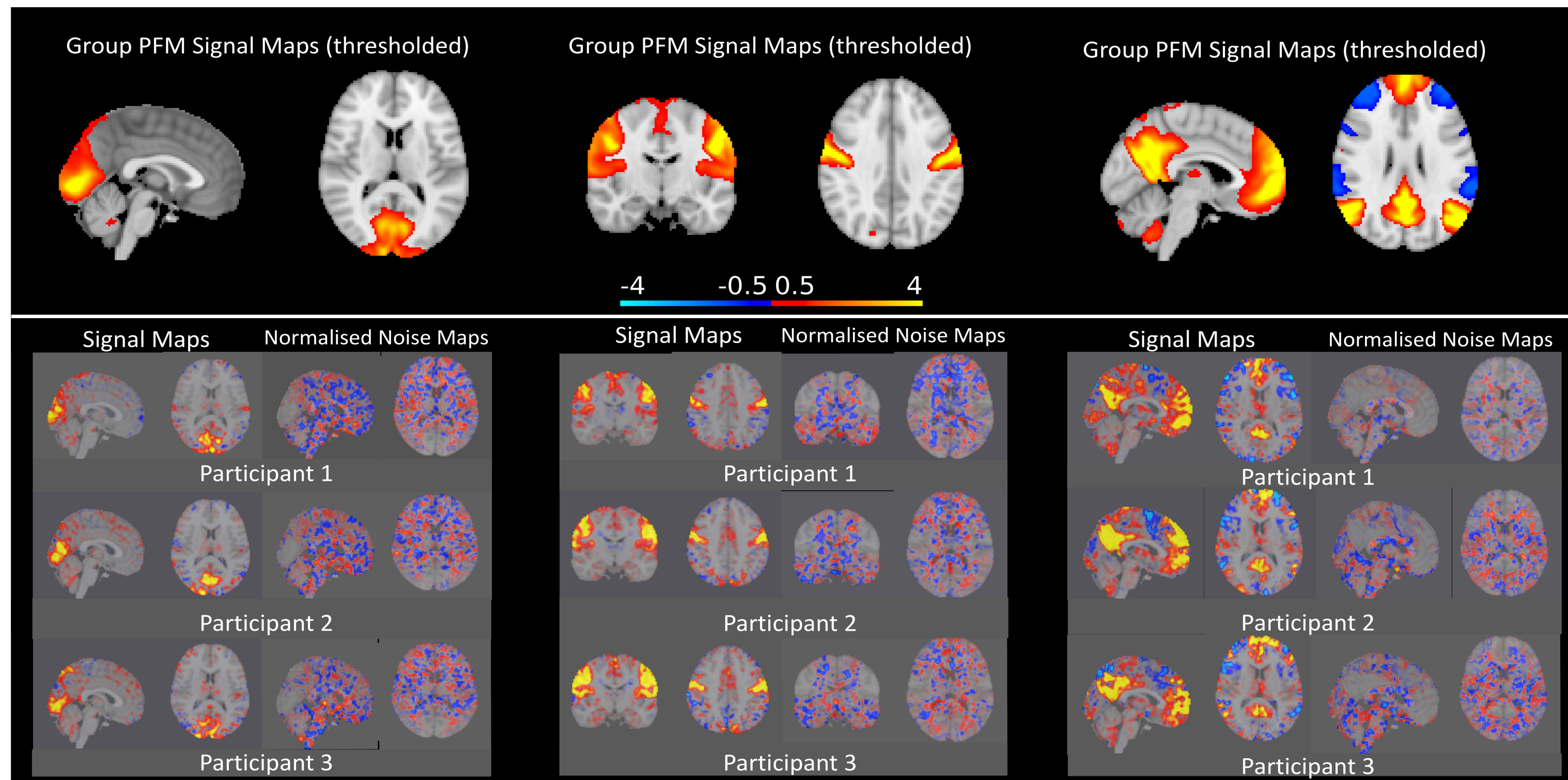


## 2) Separating *spatial* signal from background noise for subject-specific modes



To resolve this, PFMs use mixture modelling of each functional mode for each subject

- Each mode is summarised with **two** Gaussian distributions
- One distribution capturing signal, another capturing background noise

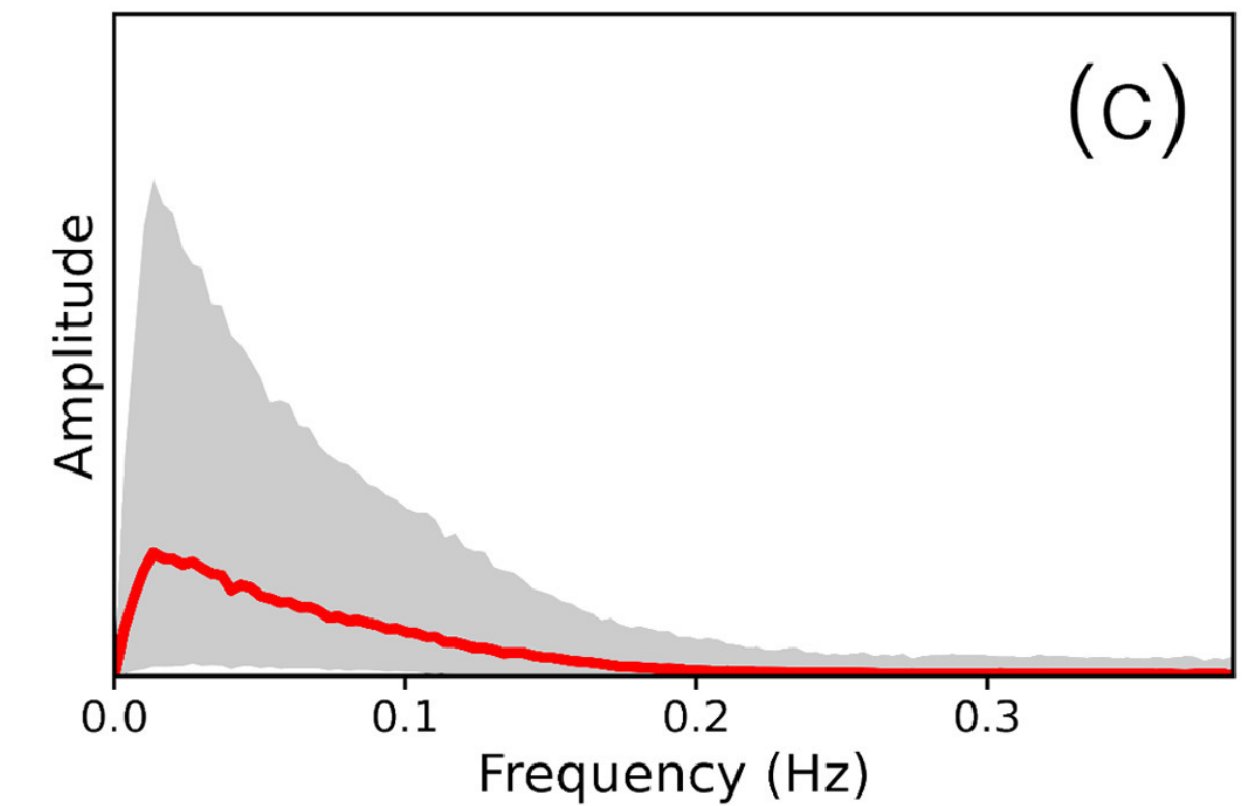
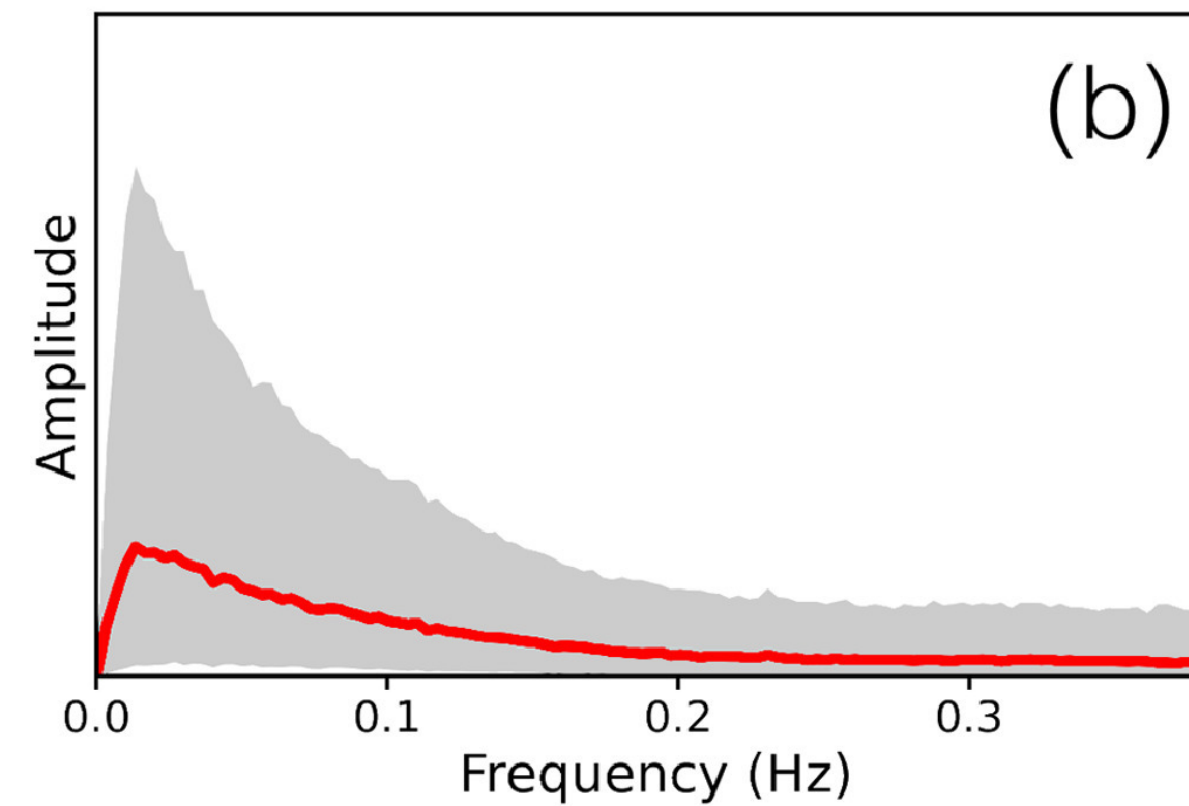
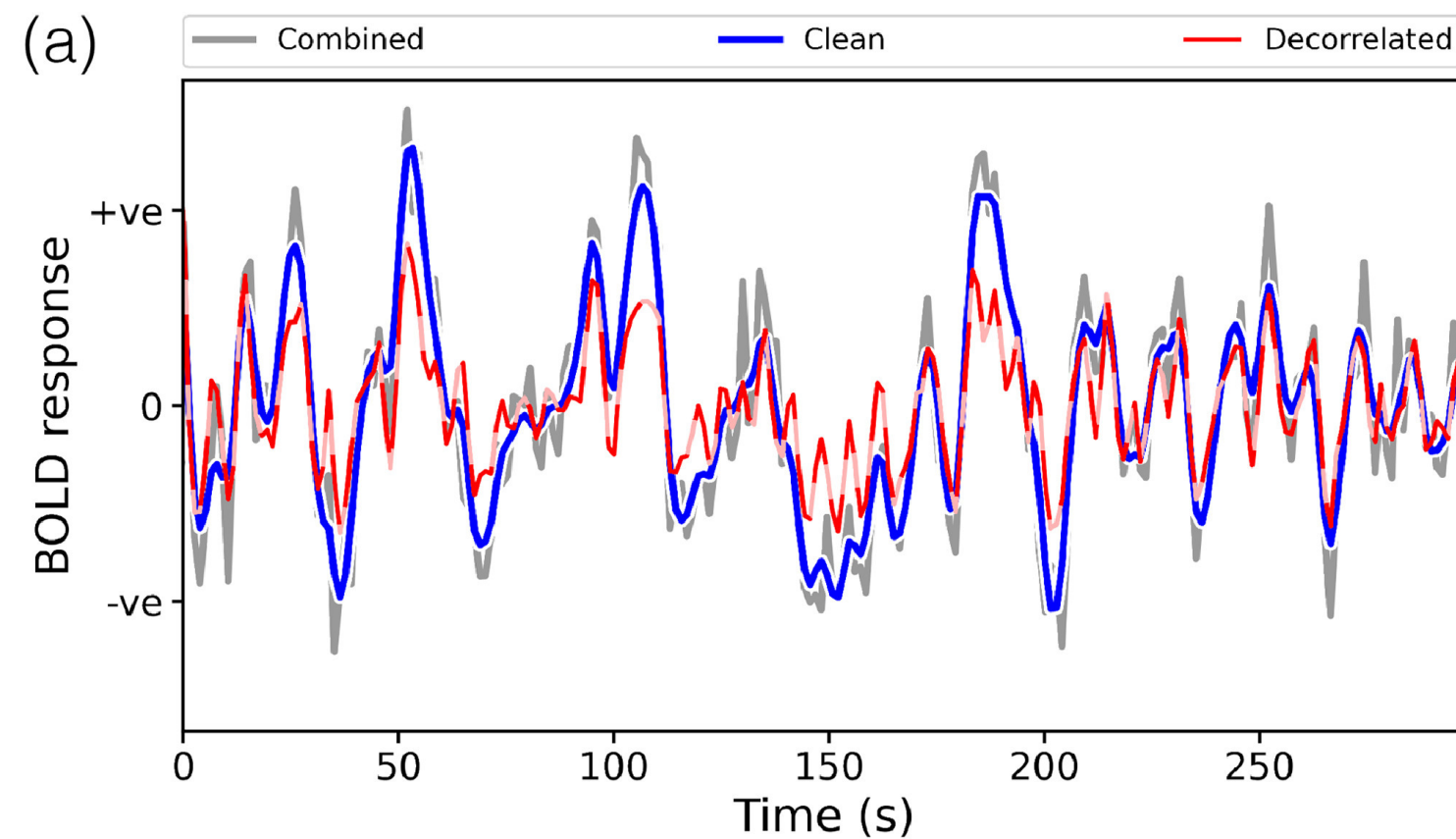


### 3) Separating *temporal* signal from background noise for subject-specific modes



Similarly, mode timecourses are separated into signal and noise subparts

- Signal part is constrained by a Haemodynamic Response Function (HRF)
- Noise part is modelled with a Gaussian distribution



Harrison et al., 2020



# Part 1 summary - in this lecture we learned that:



1. PFMs provide a unified framework to model population and every individual simultaneously
  - This is done via an iterative process, where group model is used for subject-specific regularisation and vice versa
2. To achieve this, PFMs use hierarchical Bayesian inference
  - We define probability distributions over spatio-temporal mode characteristics
  - Our aim is to optimise these distributions to explain the data, thus obtaining probabilistic functional modes
  - Hierarchy defined over spatial maps and functional connectivity (NetMats)
3. This framework provides the following advantages:
  - Group model capturing more variability
  - More accurate modelling of subject deviation from the group
  - Separating spatial and temporal Signal from background Noise to obtain 'clean' subject modes

Thank you!