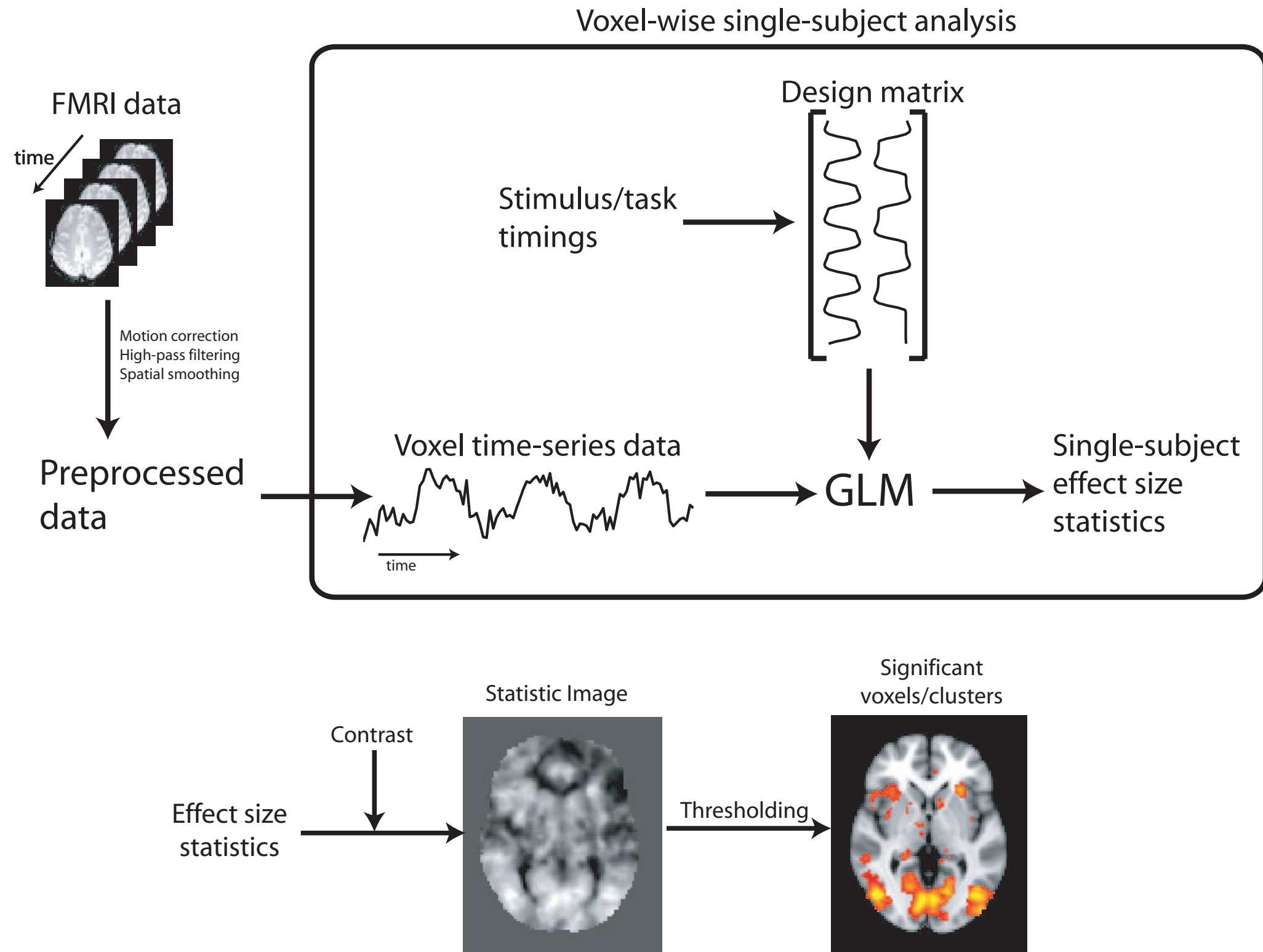




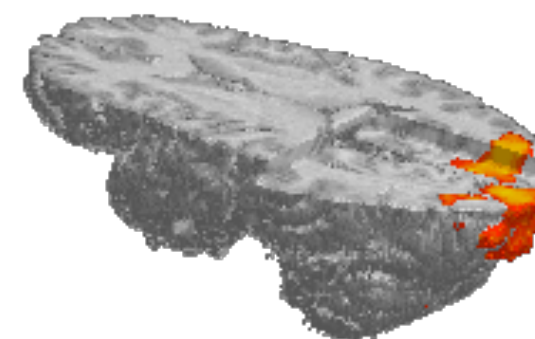
Single-Session Analysis





FMRI Modelling and Statistics

- An example experiment
- Multiple regression (GLM)
- T and F Contrasts
- **Null hypothesis testing**
- The residuals
- Thresholding: multiple comparison correction



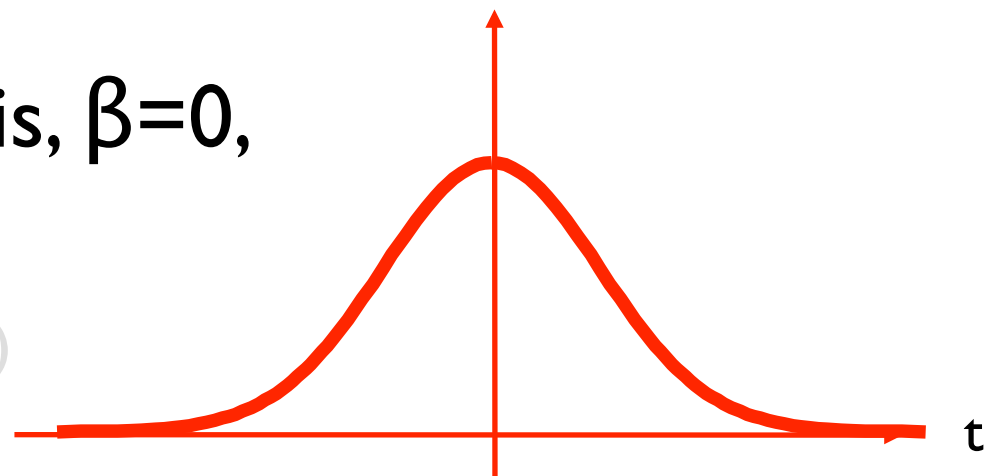


Null Hypothesis Testing

t-statistic: $t = \frac{\hat{\beta}}{\widehat{std(\beta)}}$

Under null hypothesis, $\beta=0$,
t is t-distributed

(what are the chances of that?)

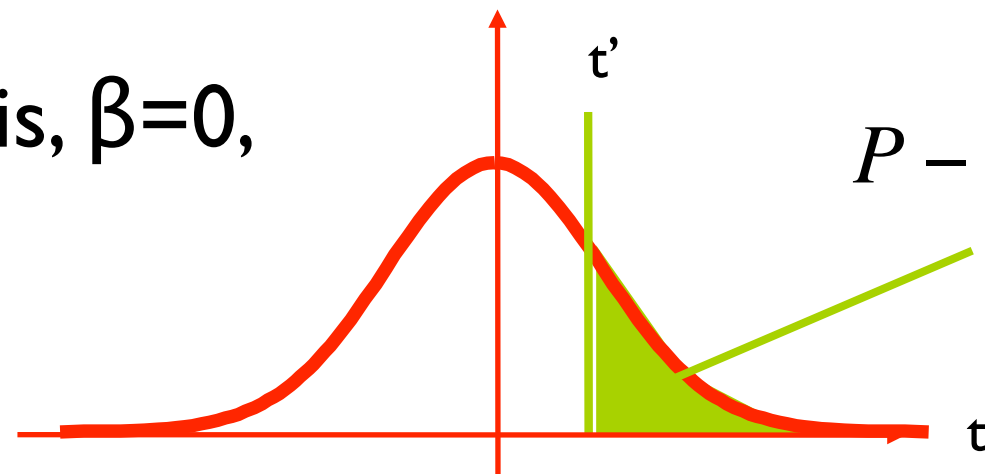




Null Hypothesis Testing

t-statistic: $t = \frac{\hat{\beta}}{\widehat{std}(\beta)}$

Under null hypothesis, $\beta=0$,
 t is t-distributed



$$P\text{-Value} = p(t > t' | \beta = 0)$$

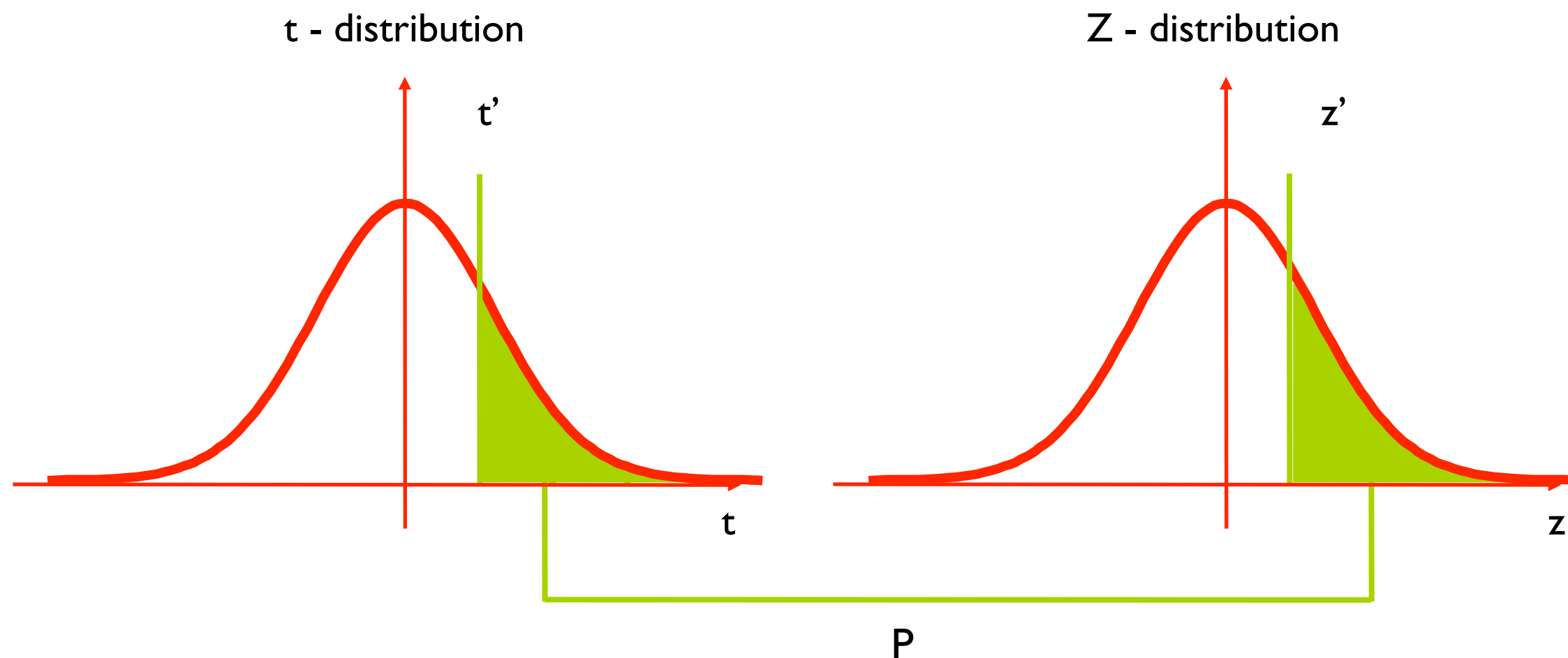
Small P-Value = null hypothesis unlikely

If P-Value < P-threshold then voxel is “active”

P-threshold corresponds to False Positive Rate (FPR)



T to P to Z

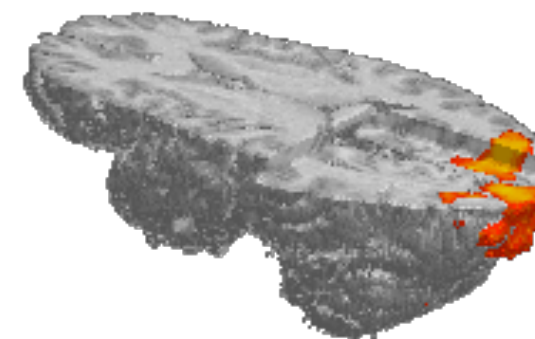


- FEAT performs spatial inference on z statistic maps
- Therefore, we convert t statistics to z statistics by equating probabilities under the tails of the distributions ($t' \rightarrow p \rightarrow z'$)



FMRI Modelling and Statistics

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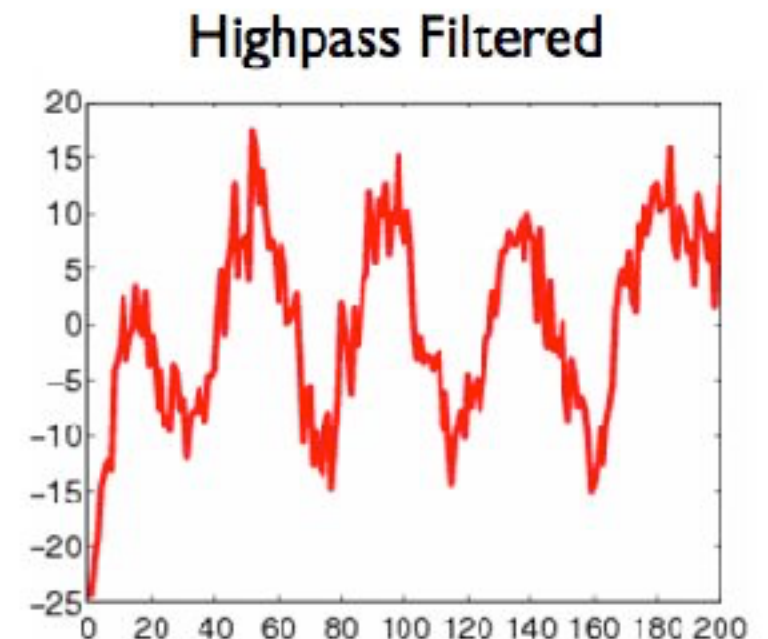
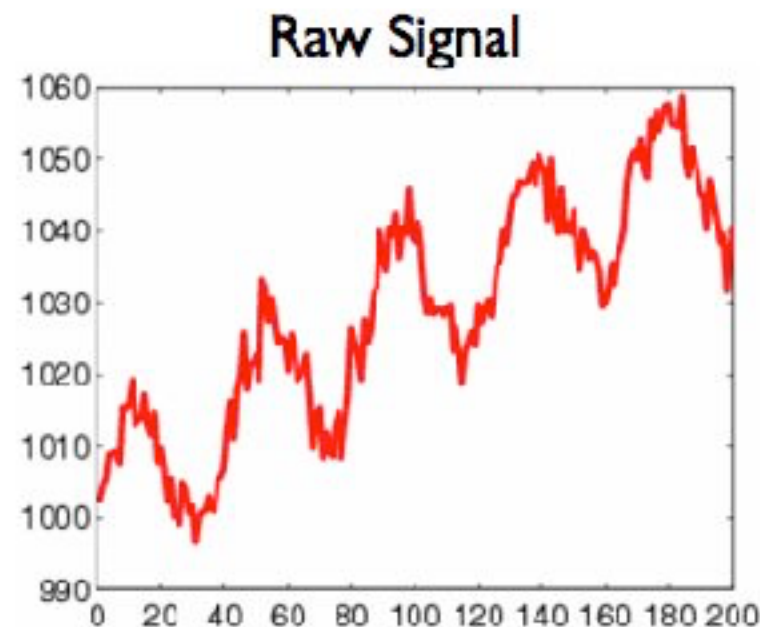
Choosing High-Pass Filter Cut-off

- Can use the tool *cutoffcalc* to determine a good cut-off value

Remember that
MJ mentioned
highpass filtering?



Temporal Filtering: Highpass



- Removes low frequency signals, including linear trend
- Must choose cutoff frequency carefully (lower than frequencies of interest = longer period)

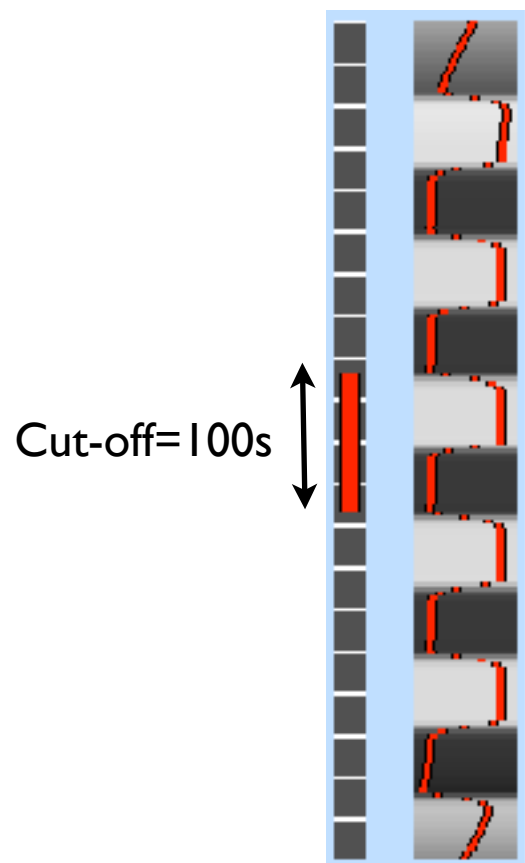


Choosing High-Pass Filter Cut-off

- Can use the tool *cutoffcalc* to determine a good cut-off value
OR
- Set by hand, but make sure model is not badly affected

Example: Boxcar EV with period

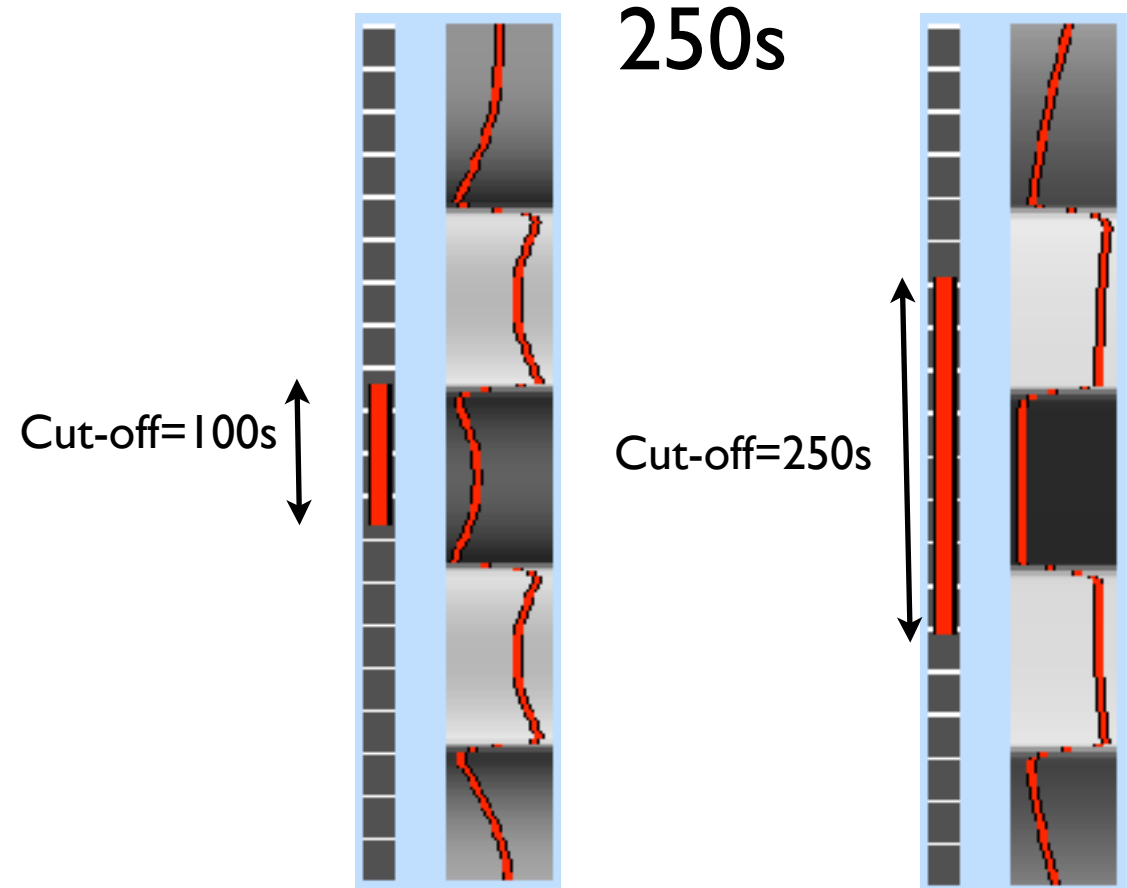
100s



Negligible effect on
EV, so use cut-off of
100s

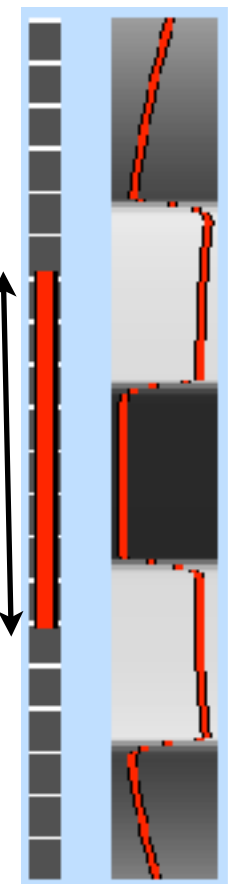
Example: Boxcar with period

250s



Substantial effect
on EV, so need
longer cut-off

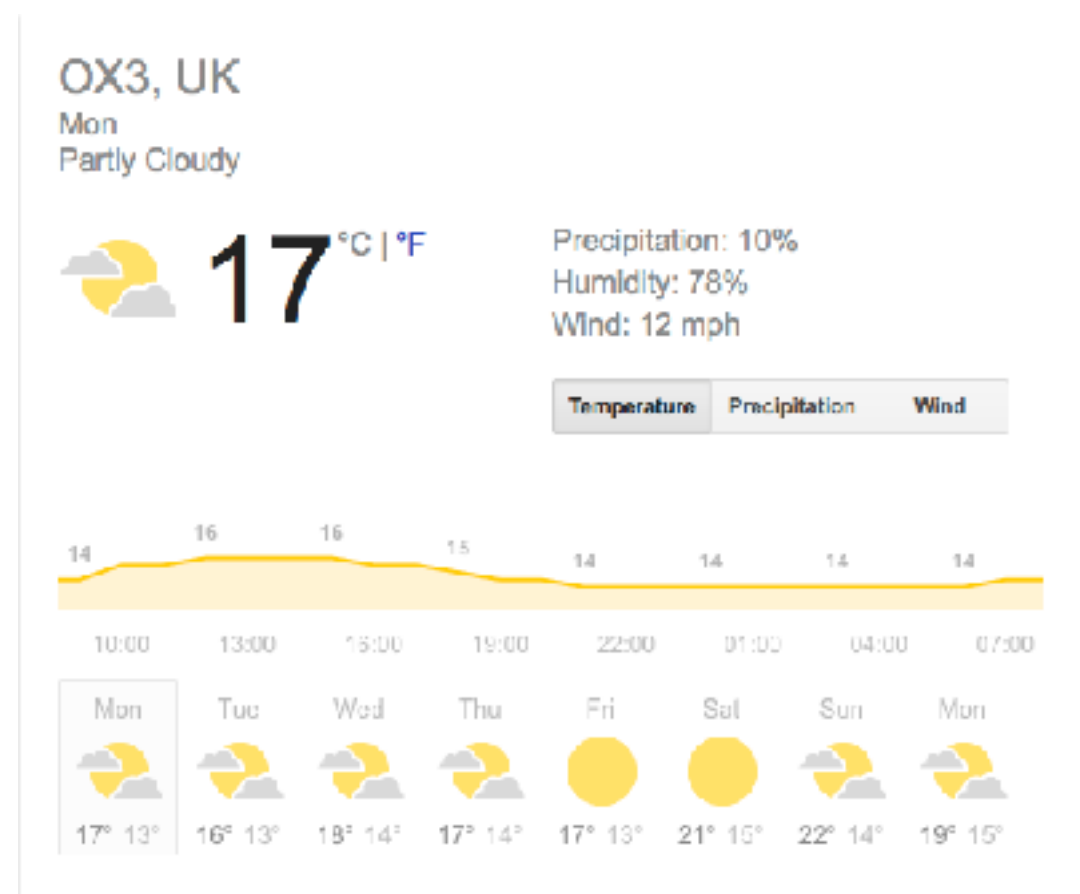
Cut-off=250s



Negligible effect on
EV, so use cut-off of
250s



Non-independent/Autocorrelation/ Coloured FMRI noise



Uncorrected, this causes:

- biased stats (increased false positives)
- decreased sensitivity

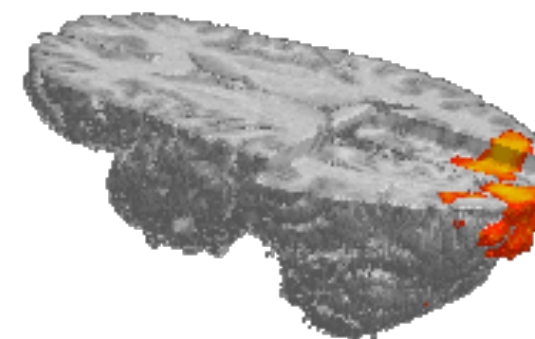
FSL fixes it for you in FEAT!

Cannot use randomise (see later) because of autocorrelation



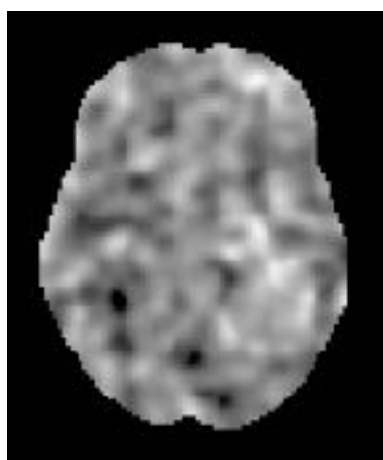
FMRI Modelling and Statistics

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- **Thresholding: multiple comparison correction**

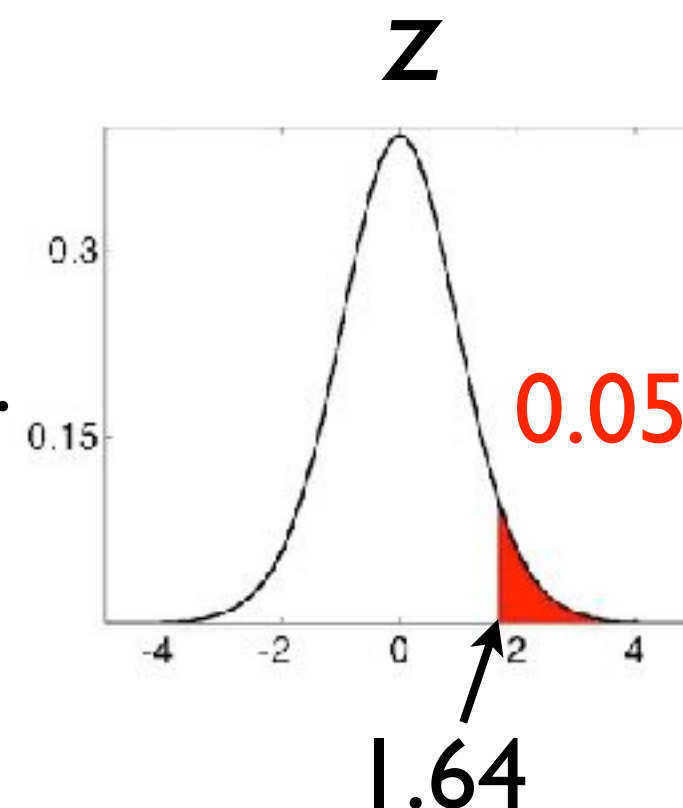




What happens when we apply “standard” statistical testing to imaging data?



z-map where each voxel $\sim N$.
Null-hypothesis true everywhere, i.e.
NO ACTIVATIONS



z-map
thresholded at
1.64



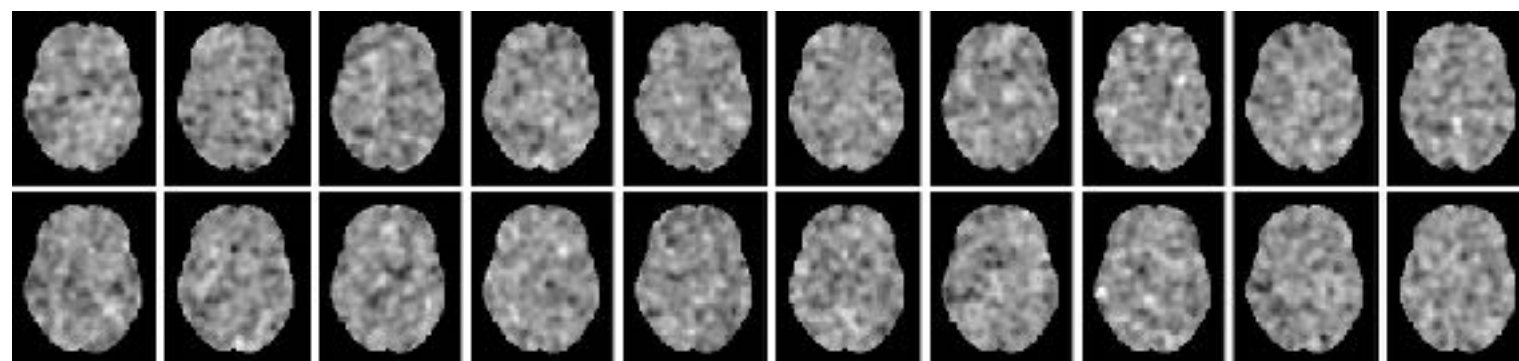
16 clusters
288 voxels
~5.5% of the voxels

That's a LOT of false positives



What we really want

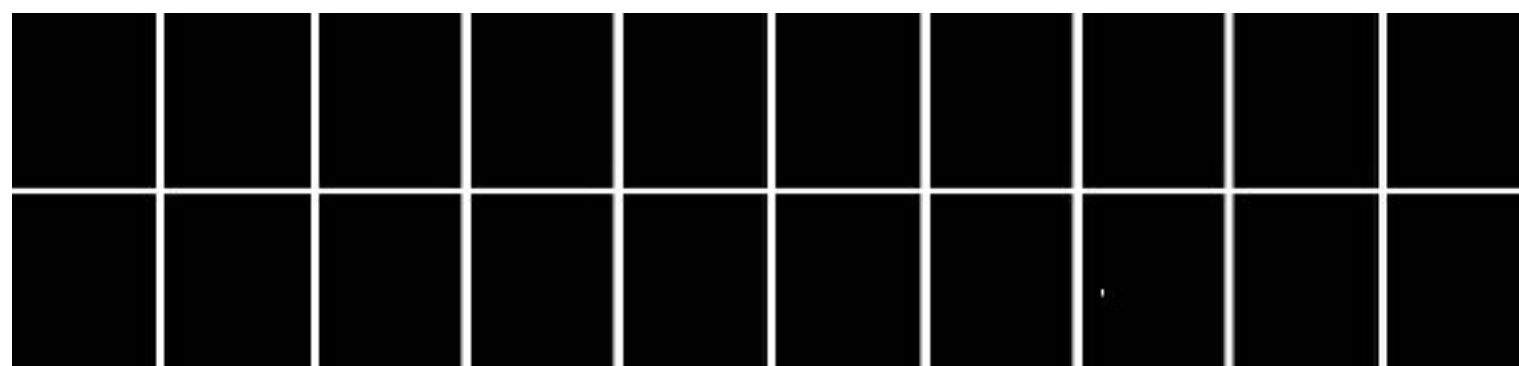
Let's say we perform a series of identical studies



Each z-map is the end result of a study

Let us further say that the null-hypothesis is true

We want to threshold the data so that only once in 20 studies do we find a voxel above this threshold



There will be a whole talk on how to find such a threshold



Summary

- We test for an effect through a null-hypothesis, that we might reject.
- The null-hypothesis is rejected if the observed statistic is “too unlikely”.
- When thresholding the number of false positives needs to be controlled across the entire brain

That's all folks

