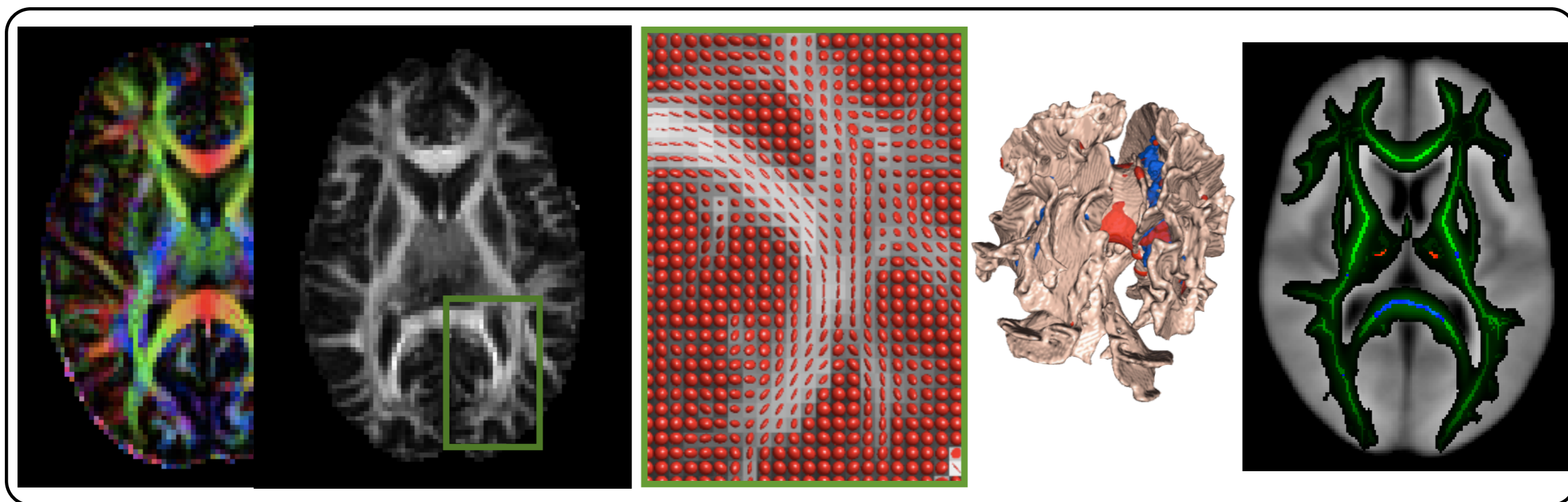


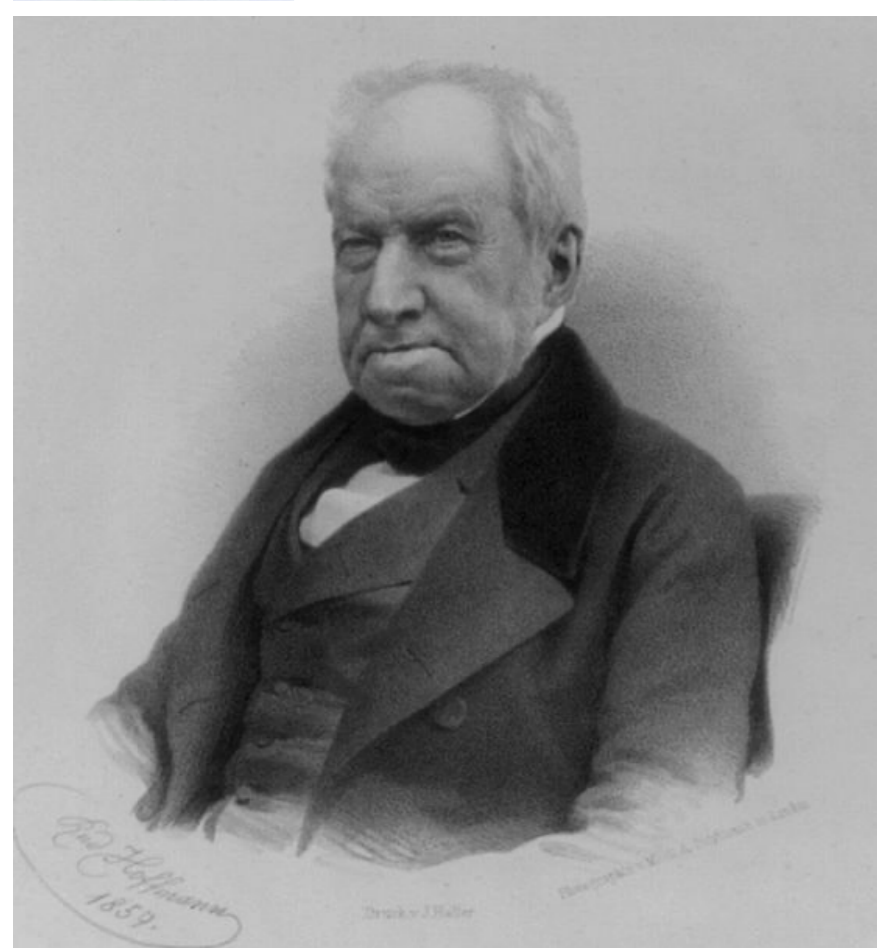


Introduction to Diffusion MRI

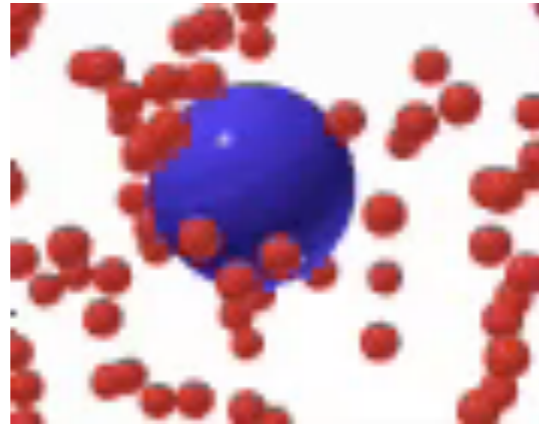




Diffusion - Brownian Motion



Robert Brown (1773-1858)**



Molecules are in constant motion at non-zero absolute temperatures ($> -273^{\circ}\text{C}$)

Diffusion = thermally-driven random motion

**Rudolph Hoffmann / Public domain
https://commons.wikimedia.org/wiki/File:Robert_Brown.jpg



Diffusion - Brownian Motion



Albert Einstein (1879-1955)**

How can we describe this motion?
For an ensemble of molecules, in n -dimensional space:

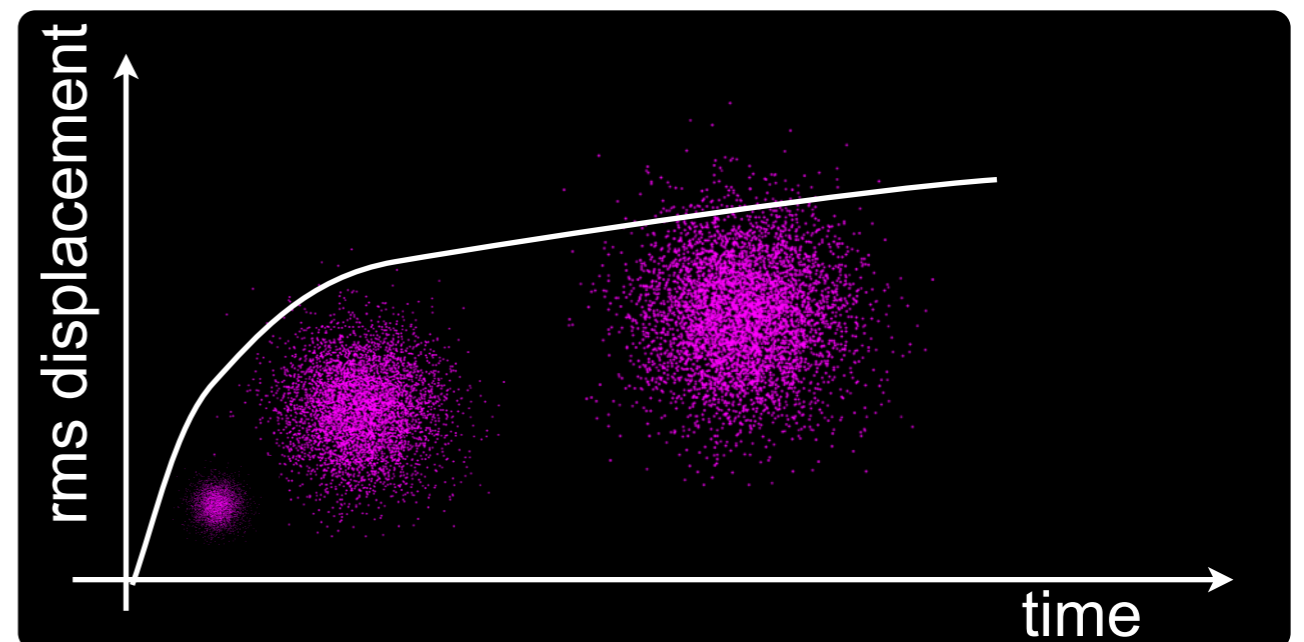
$$\langle x^2 \rangle = 2nDt$$

mean squared displacement

Diffusion coefficient

time

Valid for a homogeneous, barrier-free medium.

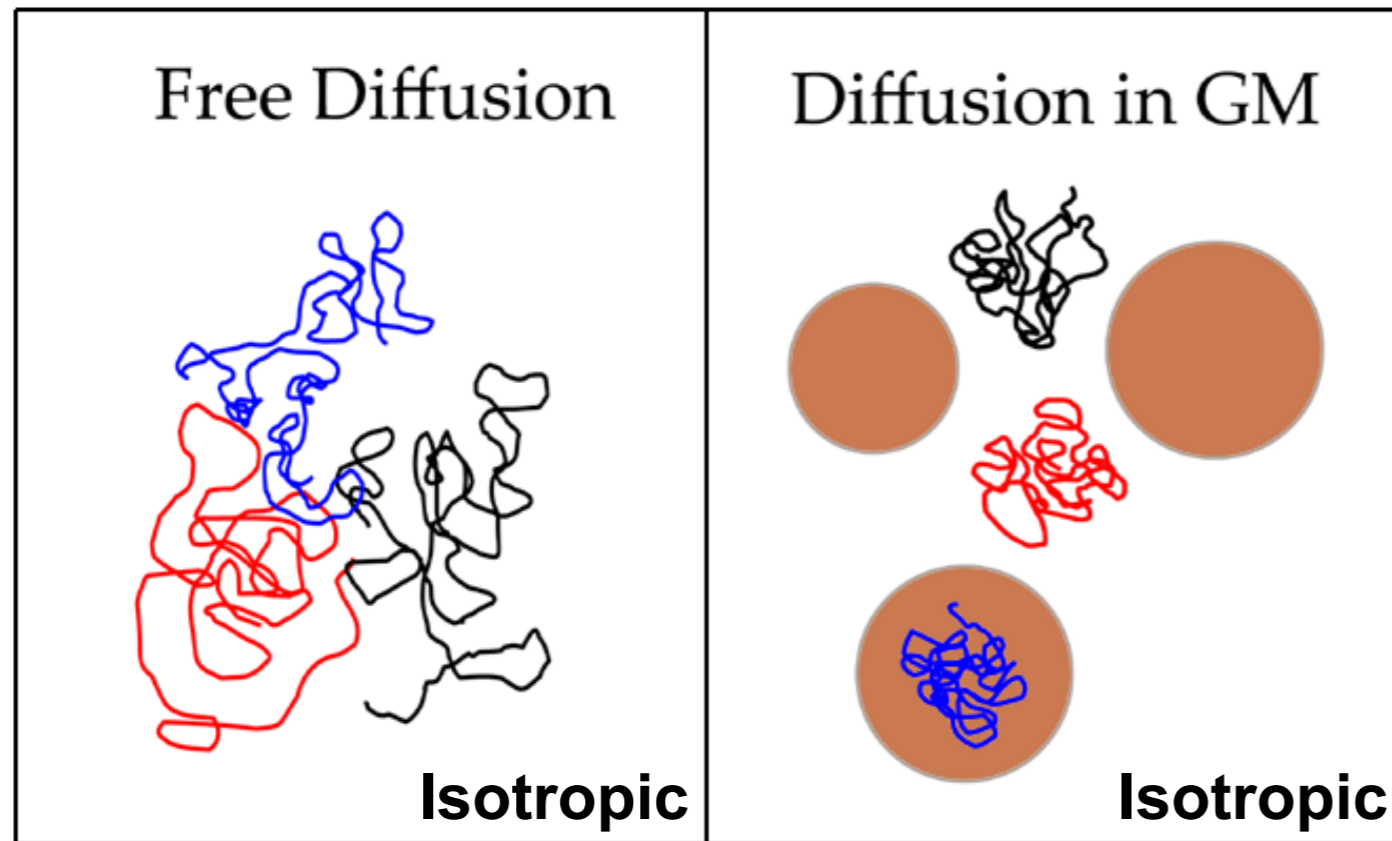


** https://commons.wikimedia.org/wiki/File:Einstein_patentoffice.jpg
Lucien Chavan / Public domain

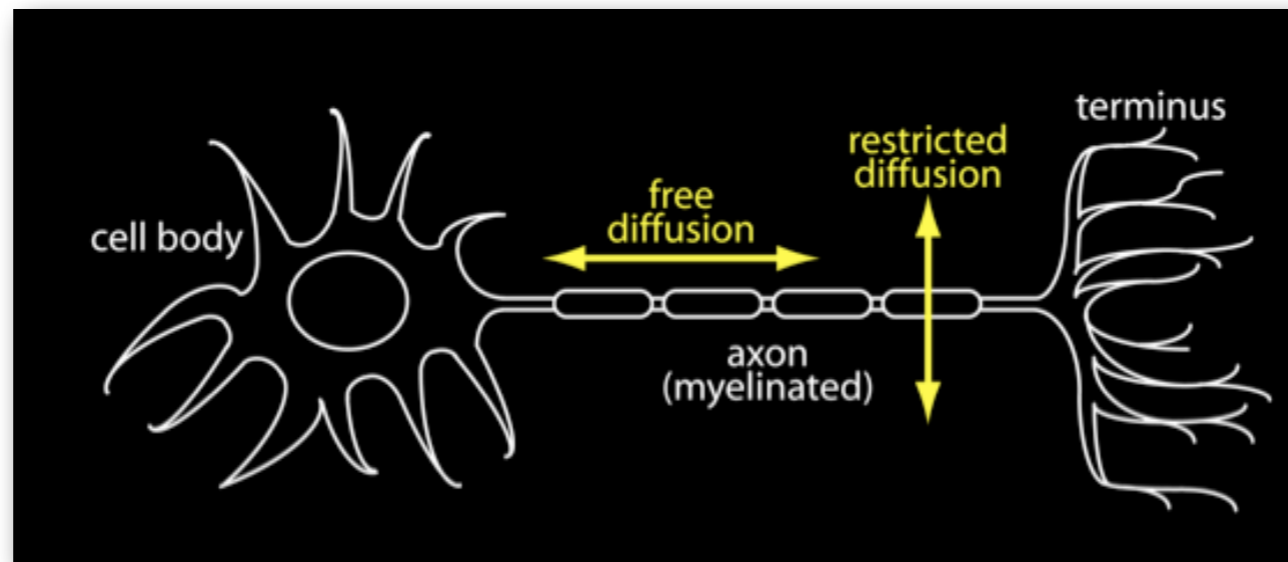
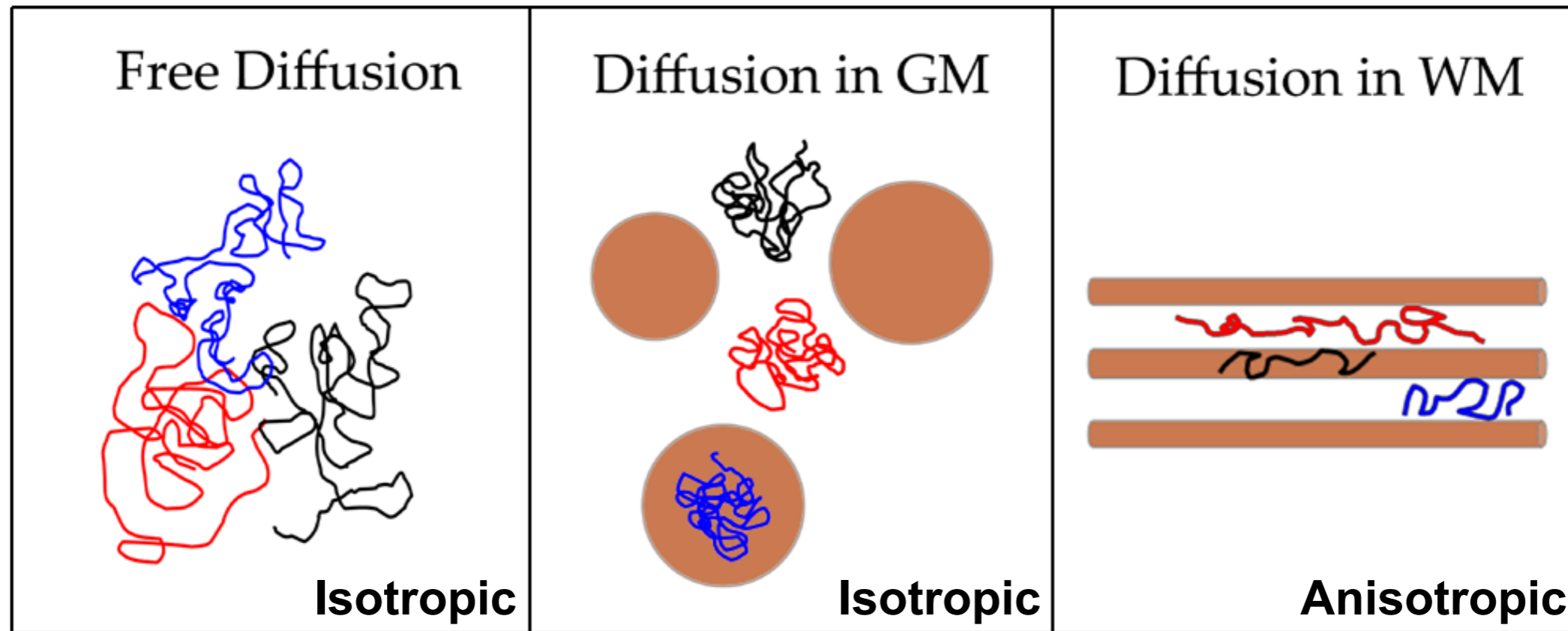
Water Diffusion in the Brain. Why is it Interesting?



Water Diffusion in the Brain. Why is it Interesting?



Water Diffusion in the Brain. Why is it Interesting?

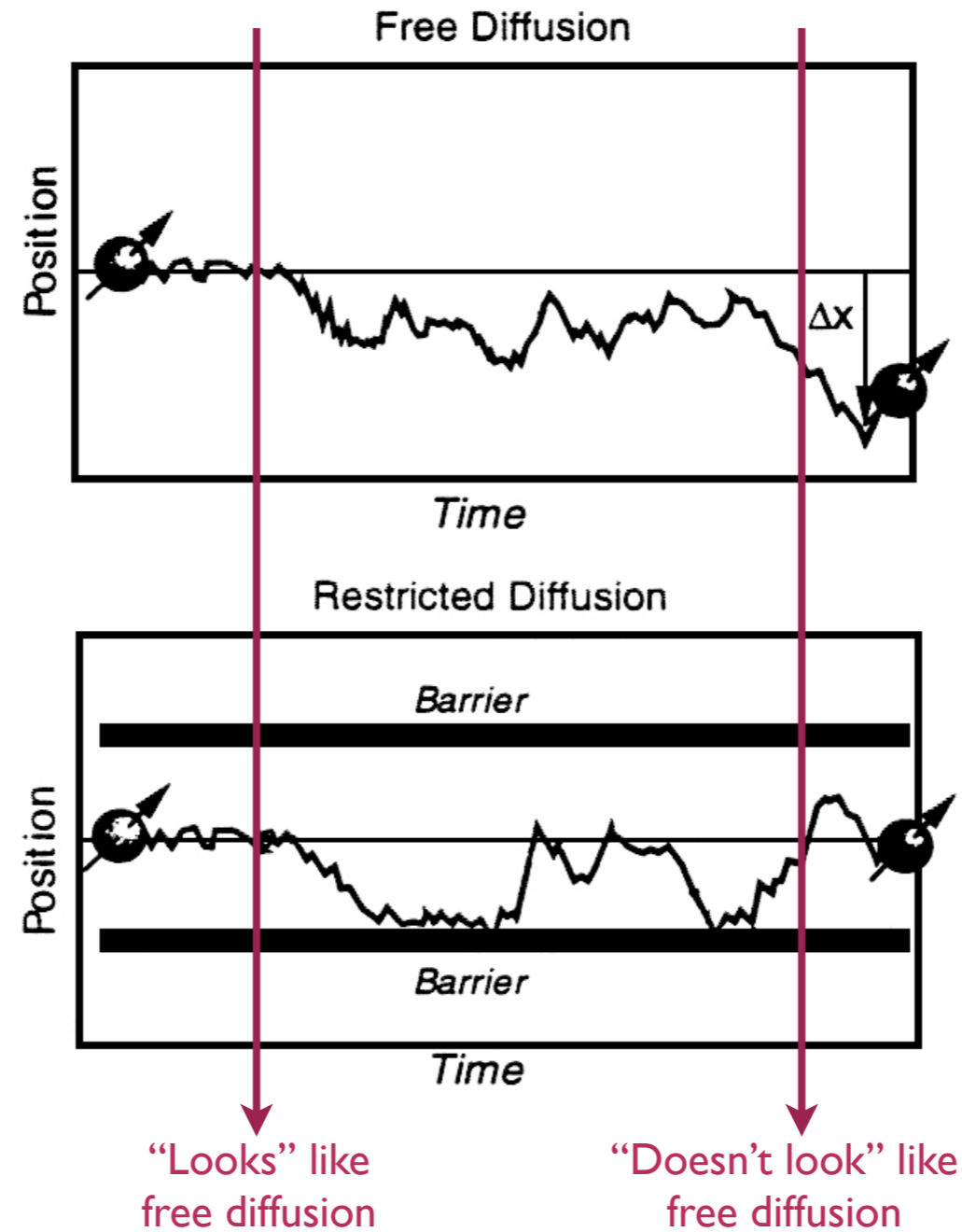


Diffusion is restricted by tissue boundaries, membranes, etc.
Marker for tissue microstructure (healthy and pathology)
Diffusion is **anisotropic** in white matter

[Beaulieu, NMR Biomed, 2002]



Apparent Diffusion Coefficient (ADC)



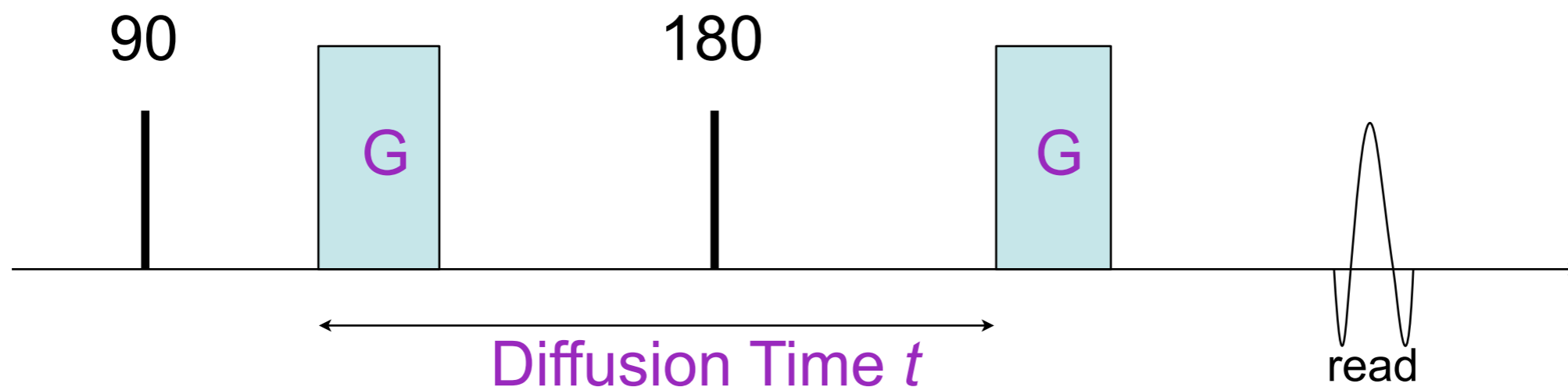
Apparent diffusion coefficient depends on the experimental details (e.g., diffusion time)



Measuring Diffusion with MRI: Diffusion MRI (dMRI)

Pulsed-Gradient Spin-Echo Sequence:

To achieve diffusion-weighting along a direction \mathbf{x} , apply strong magnetic field gradients along \mathbf{x} .



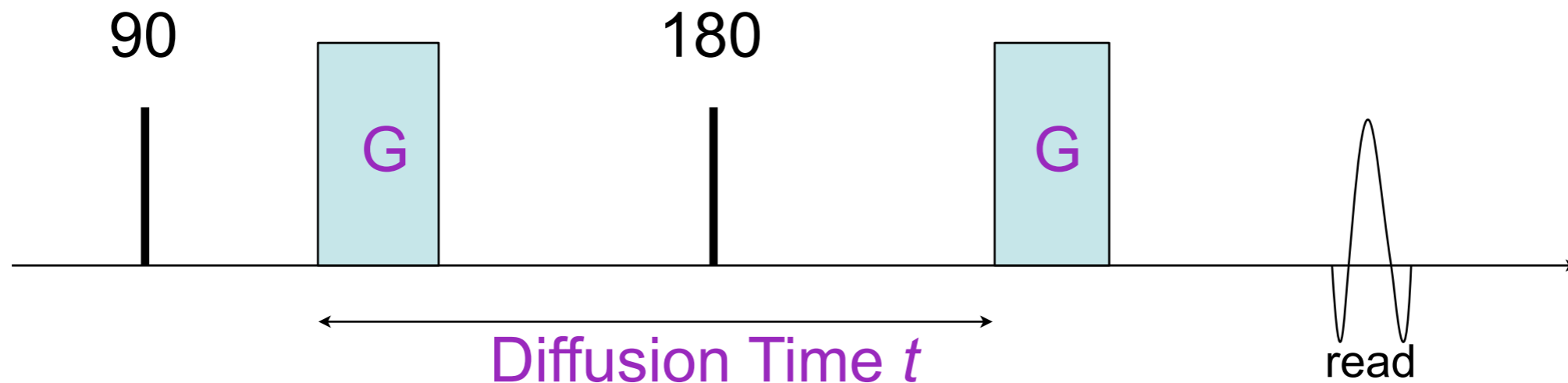
If particles diffuse along \mathbf{x} during the allowed time (DiffTime), a signal attenuation is observed, compared to the signal with $G=0$.



Measuring Diffusion with MRI: Diffusion MRI (dMRI)

Pulsed-Gradient Spin-Echo Sequence:

To achieve diffusion-weighting along a direction \mathbf{x} , apply strong magnetic field gradients along \mathbf{x} .



$$D \sim 2.4 \mu\text{m}^2/\text{ms}$$
$$t \sim 50\text{ms}$$

$$x = \sqrt{6Dt} \sim 27\mu\text{m}$$

st. deviation of displacements



Measuring Diffusion with MRI: Diffusion MRI (dMRI)

T2w Image
No Diffusion-weighting
($G=0$)
 S_0



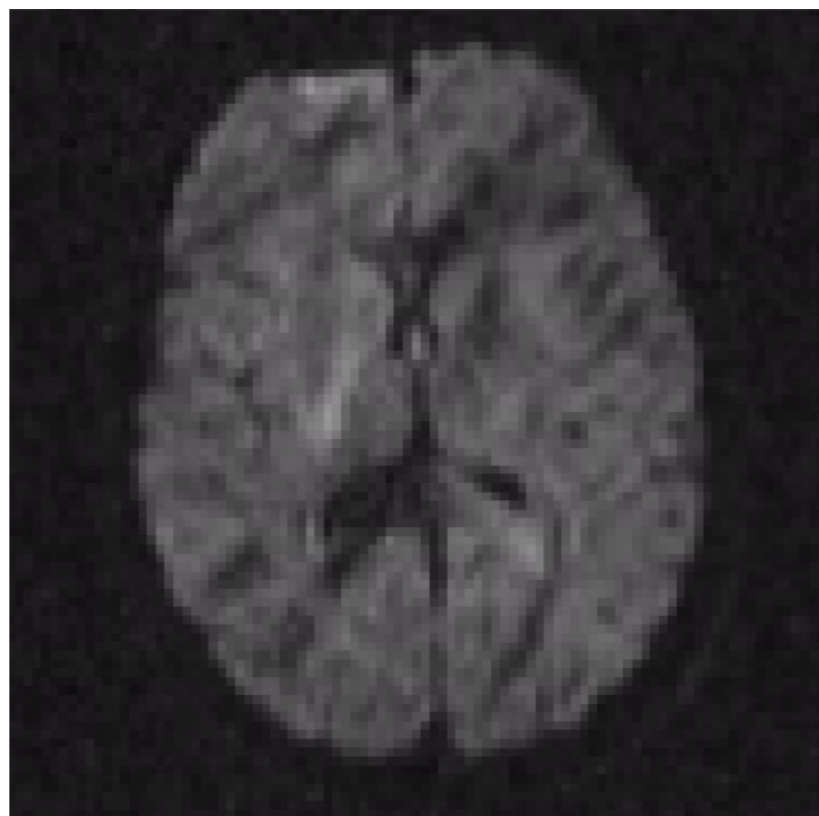


Measuring Diffusion with MRI: Diffusion MRI (dMRI)

T2w Image
No Diffusion-weighting
($G=0$)
 S_0



Diffusion-weighted
Image
 S



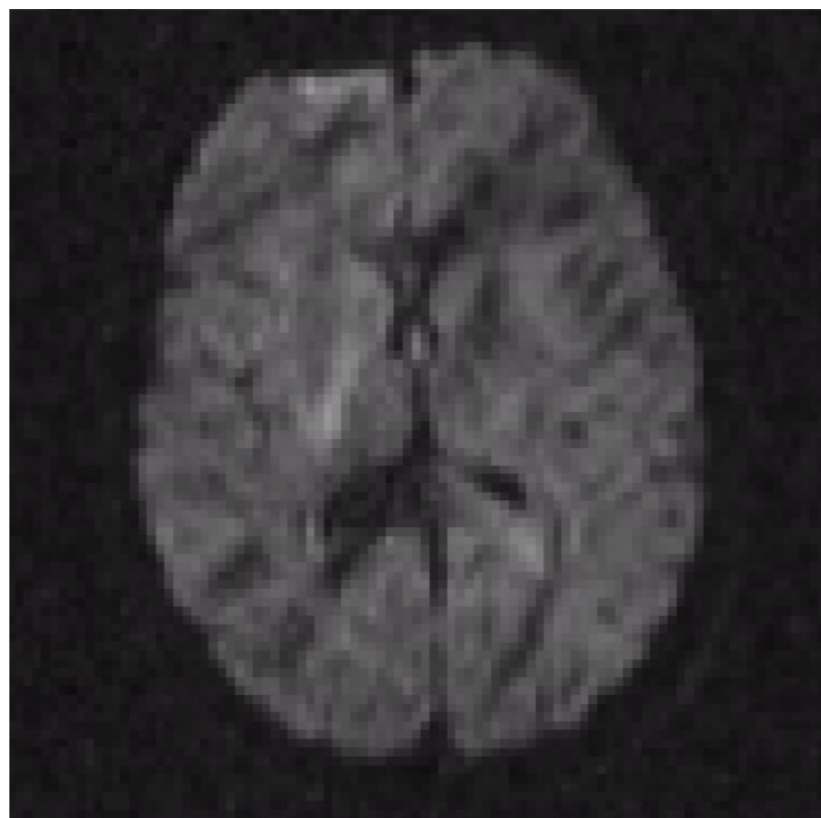


Measuring Diffusion with MRI: Diffusion MRI (dMRI)

T2w Image
No Diffusion-weighting
($G=0$)
 S_0



Diffusion-weighted
Image
 S



Ratio
 S/S_0



Removes T2w contrast



Measuring Diffusion with MRI: Diffusion MRI (dMRI)

Diffusion contrast can be modulated by:

A) Diffusion weighting: Gradient **strength**, Diffusion **time**

$$\mathbf{b\ value} \sim G^2 \cdot \text{DiffTime} \quad (\text{units in s/mm}^2)$$



Measuring Diffusion with MRI: Diffusion MRI (dMRI)

Diffusion contrast can be modulated by:

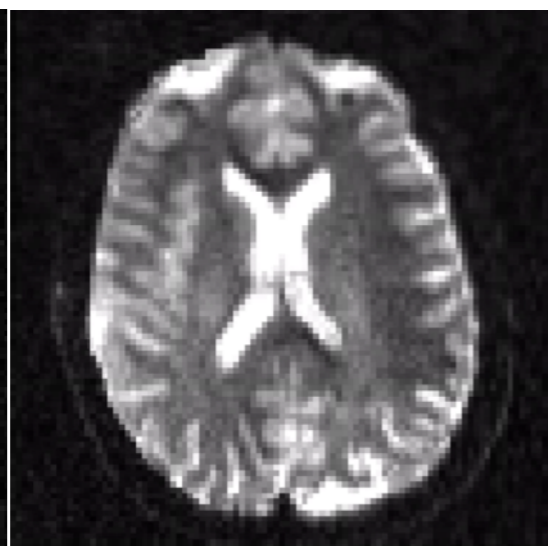
A) Diffusion weighting: Gradient **strength**, Diffusion **time**

$$\mathbf{b\ value} \sim G^2 \cdot \text{DiffTime} \quad (\text{units in s/mm}^2)$$

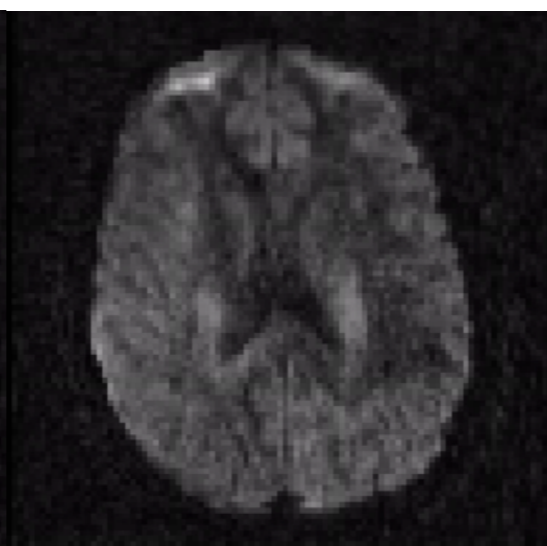
b=0



b=300



b=1000



b=2000



b=3000

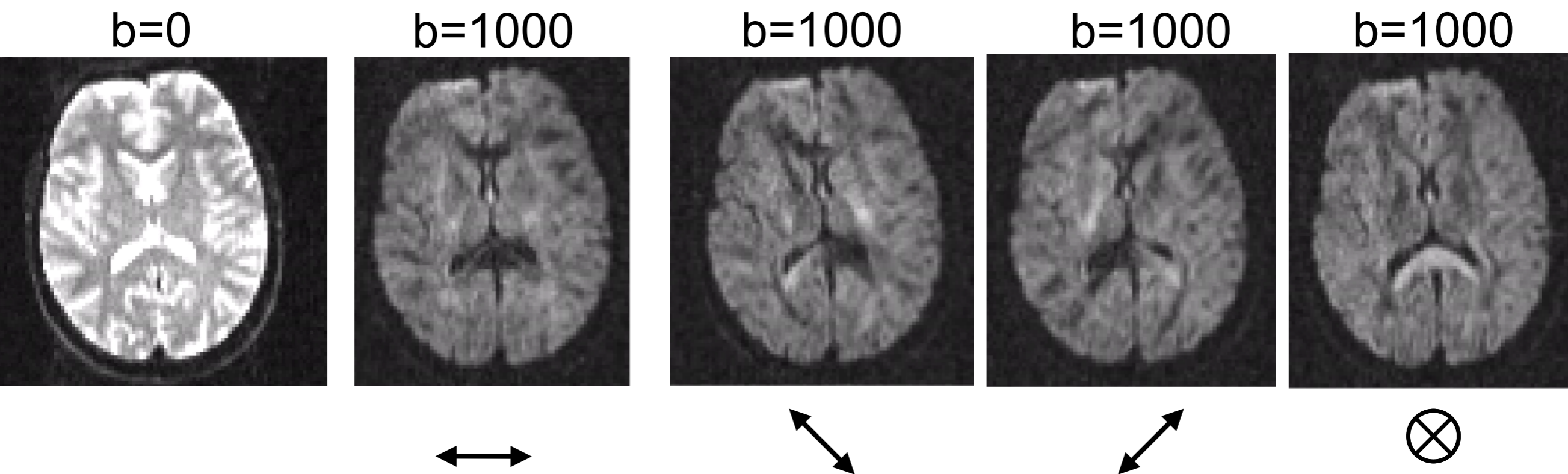


More diffusion contrast with higher b :)
...But less signal left - exponential decay :(



Measuring Diffusion with MRI: Diffusion MRI (dMRI)

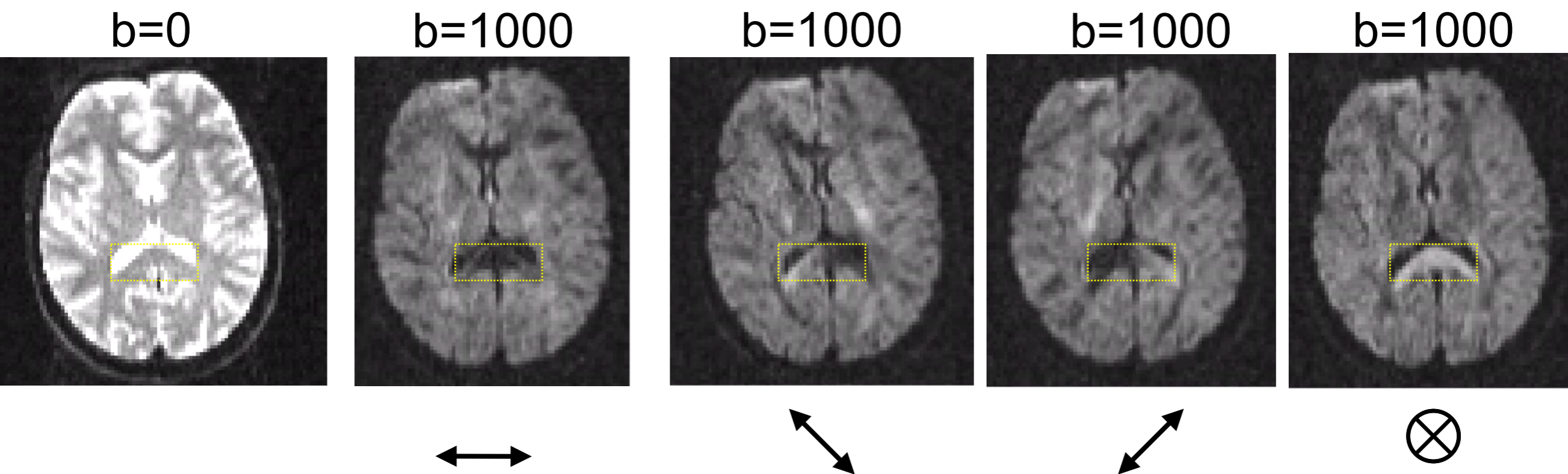
Diffusion contrast can be modulated by:
B) Gradient Direction





Measuring Diffusion with MRI: Diffusion MRI (dMRI)

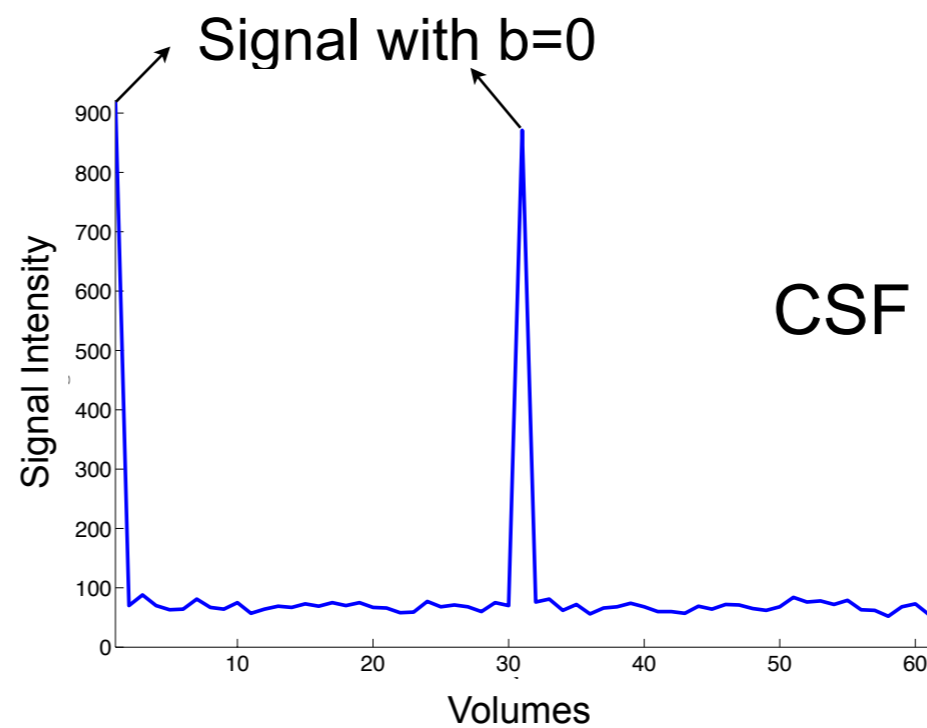
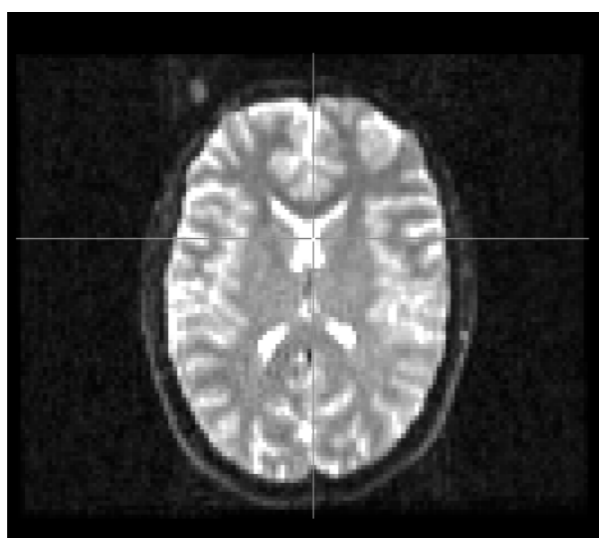
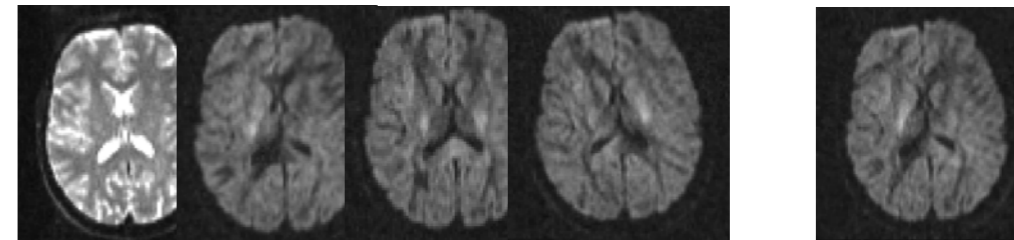
Diffusion contrast can be modulated by:
B) Gradient Direction





A Typical dMRI Protocol

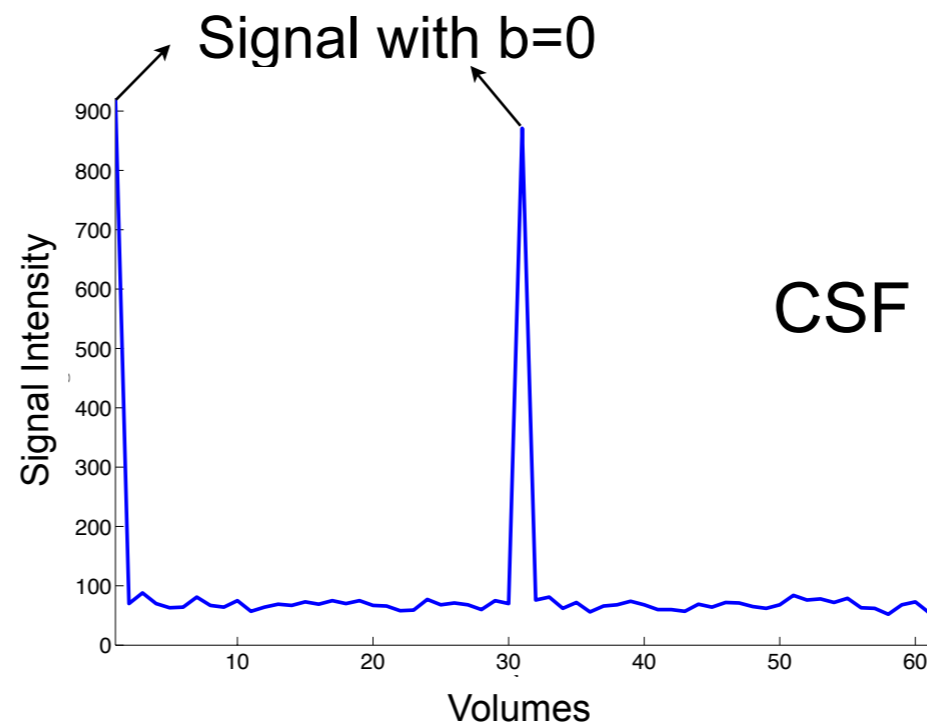
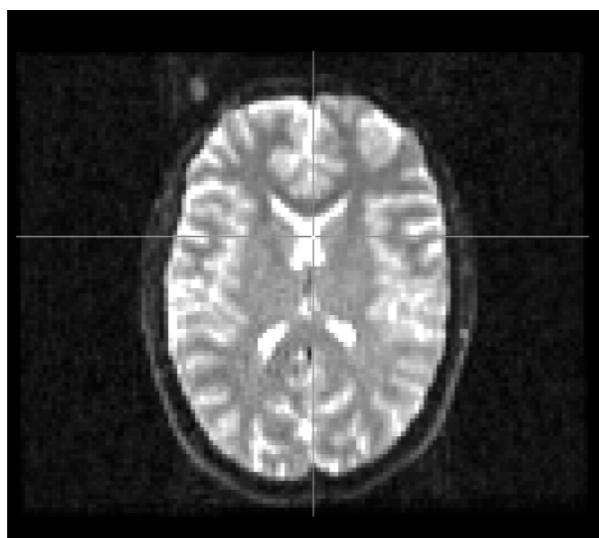
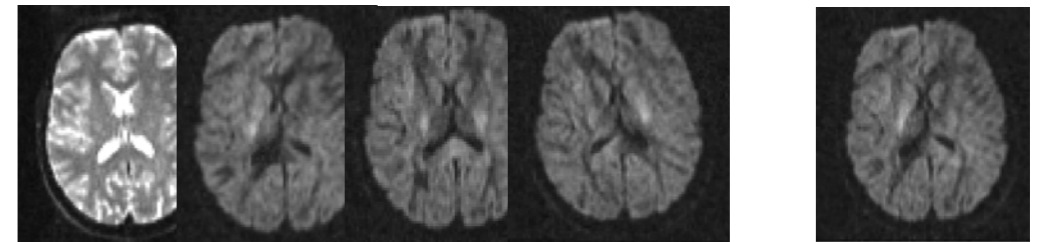
- Normally a few (at least one) $b=0$ volumes acquired, along with volumes at higher b (~ 1000 s/mm^2).
- Different gradient directions are applied for the high b volumes.



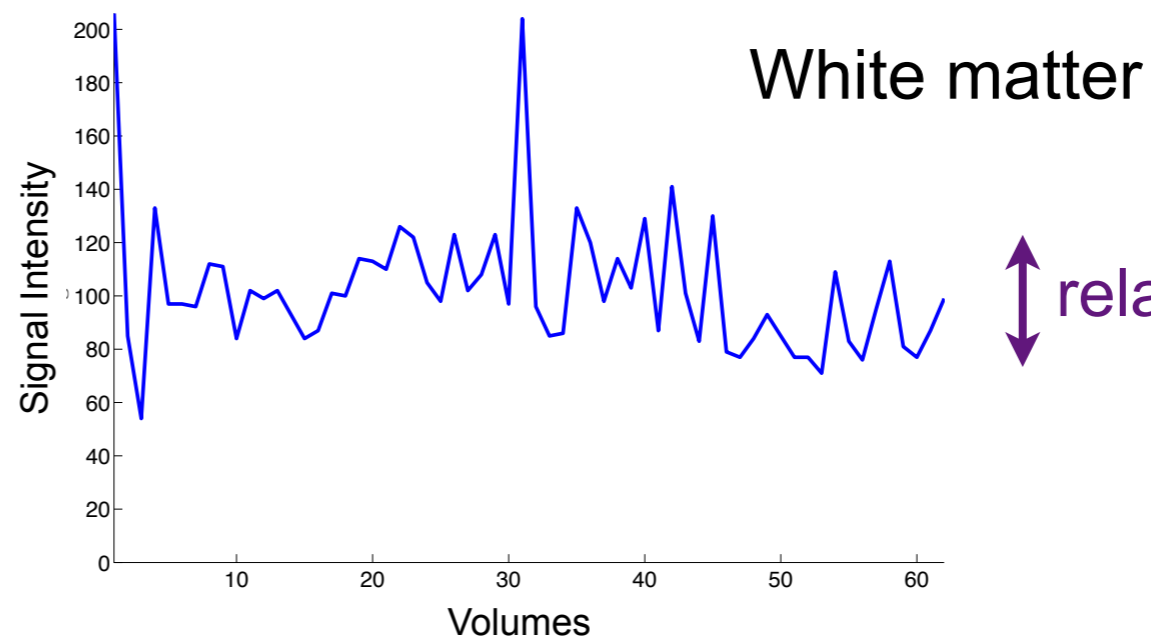


A Typical dMRI Protocol

- Normally a few (at least one) $b=0$ volumes acquired, along with volumes at higher b (~ 1000 s/mm^2).
- Different gradient directions are applied for the high b volumes.



relates to ADC



relates to anisotropy



dMRI Summary

- Images acquired with a Gradient along direction \mathbf{x} , have contrast that is sensitive to diffusion of water molecules along direction \mathbf{x} .
- When diffusion occurs, signal is attenuated compared to no diffusion-weighting.
- In WM, measurements are anisotropic. There is a preferred direction of diffusion.
- In GM and CSF, measurements are roughly isotropic.